

*Full Length Research Paper*

# **Review of the mathematical thinking levels of gifted and non-gifted students**

**Zübeyde ER**

Çukurova Science and Art Center, Turkey.

Received 18 August, 2023; Accepted 13 September, 2023

**This study aimed to determine the mathematical thinking levels of gifted and non-gifted students and to compare them according to some variables. In this study, screening model was used from quantitative research methods. The study group of the study consists of 194 gifted students and 168 non-gifted students studying in grades 5-8 in a province in the southern region of Turkey in the 2022 to 2023 academic year. According to the results of the research, it was found that the mathematical thinking levels of gifted students were higher than their non-gifted peers. In addition, the mathematical thinking levels of gifted students showed a significant difference compared to grade level. This does not apply to non-gifted students. It was found that the mathematical thinking levels of female students were higher than the mathematical thinking levels of male students in gifted and non-gifted student groups, but this difference was not statistically significant. In addition, it was seen that the success grade of the mathematics course made a significant difference on the mathematical thinking level of both the gifted and non-gifted student groups.**

**Key words:** Gifted students, mathematical thinking, non-gifted students.

## **INTRODUCTION**

Today, with the rapid pace of change, the education systems of the countries make it an important goal to educate students in a way that they dominate technology and contribute to their country by directing the change in the world. Education systems shaped in this direction will be successful when they can raise individuals who can offer different and qualified answers to original problems in daily life by using current opportunities in the most effective and efficient way. For this reason, curricula take into account the development of 21st century basic skills

and attach importance to learning processes that can provide this. Mathematical thinking is one of the basic skills that the nations want to gain in the qualified educational environments targeted by the nations and that the nations integrate into their curricula. The mathematics curriculum, which was revised by the Ministry of National Education in Turkey, started to be implemented in all grade levels of primary and secondary schools as of the 2018-2019 academic year. It is stated that instead of a structure that only conveys information

E-mail: [zbeyde-er@windowslive.com](mailto:zbeyde-er@windowslive.com).

Author(s) agree that this article remain permanently open access under the terms of the [Creative Commons Attribution License 4.0 International License](https://creativecommons.org/licenses/by/4.0/)

in the new curriculum, a simple structure that takes into account individual differences, focuses on gaining values and skills is aimed. In addition, it is stated that it is aimed to raise individuals with knowledge, skills and behaviors integrated with values and competencies (MEB, 2018). This study focused on examining the mathematical thinking levels of gifted and non-gifted student groups in terms of different variables. Thus, it was thought that it would be important to reveal the reflection of the achievements of mathematical thinking skills in the mathematics teaching curriculum to the students.

### Mathematical thinking

Mathematics has its own language and way of thinking. Since mathematics is a systematic structure, mathematical thinking has an important place in this system. Mathematical thinking skills can enable people to know themselves and the universe as a common thinking tool. Individuals who have acquired mathematical thinking skills can be successful in solving problems related to themselves and their environment (Tall, 1991). The importance of mathematical thinking emerges at this point, as appropriate responses to problems will be achieved with a sound and functional thinking skill (Yenilmez, 2007). Mathematical thinking helps individuals to realize the place and importance of mathematics in the world, to be constructive, reflective and sensitive citizens and to make sound decisions (PISA, 2015). In fact, mathematics, beyond all this, is often considered as life itself. Learning mathematics requires learning basic concepts and skills, as well as thinking mathematically, solving problems, and understanding that mathematics is important in real life.

The development of the concept of mathematical thinking in education and the importance of highlighting this skill in the learning process began in the 1980s, and Egan (1975), Freudenthal (1981), Krutetskii (1976), Burton (1984) and Schoenfeld (1992) studies reveal how important mathematical thinking is in mathematics education. Although there is no common definition and set of components for the concept of mathematical thinking in the field literature, it can be seen that mathematical thinking is a high-level thinking process that requires the management of processes that will solve the problem situation other than finding only the answer to a problem (Polya, 1945). According to Henderson et al. (2003), mathematical thinking is the direct or indirect application of mathematical processes to solving problems. Burton (1984) stated that mathematical thinking is not thinking about the subject of mathematics, but a way of thinking that is a function of known mathematical dynamics, processes and certain processes. Liu (2003) defined mathematical thinking as "the combination of estimating, induction, generalization, sampling, deduction, description, verification, formal and

non-formal reasoning, and similar processes." Yeşildere (2006) stated that mathematical thinking occurs if high-level thinking skills such as customization, generalization, prediction, hypothesis generation, checking the accuracy of a hypothesis are required in the solution of a problem. When defining mathematical thinking, some of its elements are mentioned. Mason et al. (1985) stated that mathematical thinking consists of the processes of customization, generalization, hypothetical, and verification-persuasion, while Tall (2002) states that it consists of abstraction, synthesis, generalization, modeling, and proof. Alkan and Güzel (2005) also stated that mathematical thinking occurs by using the individual's previous knowledge of mathematics and abstraction, prediction, generalization, hypothesis and testing, reasoning and synthesis, etc.

Although mathematical thinking is perceived as a process used to solve mathematical problems, it is a process that can be used in every problem to be encountered in daily life. It is important to learn and teach mathematical thinking (Demirtaş, 2018) and to have a good mathematical thinking. In fact, mathematical thinking is one of the elements that form the basis of problem-solving skills. Similarly, Tuncay (2015) emphasized the importance and impact of mathematical thinking on the problem-solving process.

### Gifted students

Not every individual is the same in educational settings. There are individuals who think at different speeds and have different individual characteristics. One of these student groups is gifted students. Gifted students have cognitive skills that will enable them to be successful in the fields of science and art, and they constitute approximately 2% of the society (Ataman, 2004). For this reason, gifted individuals need to be well trained and guided through education prepared in accordance with their characteristics (Davis, 2006). There are different approaches to define giftedness in the field literature.

Renzulli (1978), called the three-ring model, expresses giftedness as the intersection of above-average ability, task delivery, and creativity. Gifted individuals will form the intellectual segment in the society if their potential is evaluated correctly by giving appropriate trainings to them (Bakar et al., 2018). With appropriate trainings, it is inevitable that gifted individuals will contribute positively to the development of both their immediate environment and society (Sontay et al., 2014). In Turkey, gifted people are diagnosed in 5 stages.

Stage 1: Announcement phase

Stage 2: Filling out observation forms by classroom teachers

Stage 3: Evaluation of forms

Stage 4: Group screening

## Stage 5: Individual review

The basic stages in which the diagnosis of gifted are 4th and 5th stages, in which students who succeed in the group screening are evaluated individually. In this individual evaluation, the intelligence test preferred by the Ministry of National Education is applied. In 2015, WNV, or Wechsler intelligence test, was applied to 2nd, 3rd and 4th grade students. In 2016, while Kbit or Kaufman short intelligence test was applied to the first and second grades, the WNV test was applied to the third and fourth grades. In 2017, this time, ASIS, namely SAK Intelligence Scale, was applied to first and second year students in SAC auditions, while WNV test was applied to third year students. In SAC intelligence tests, a new regulation is made every year and it is preferred to change the tests. In this context, it is not possible to talk about a certain intelligence test every year, and individuals with an IQ score of 130 and above in the tests are defined as gifted individuals. In addition to the formal education activity in their schools, individuals who are diagnosed as gifted receive education according to the talent area (General Ability, Painting, Music) in SAC. In the diagnosis, there is no process for whether individuals are gifted in the field of mathematics (Aygün et al., 2020). In addition to the (formal) mathematics teaching curriculum in their schools, gifted students also experience different teaching processes in the Science and Art Center. Since mathematical thinking is a high-level thinking activity, it is expected that gifted individuals will emerge in problem-solving processes. In this case, it is important to determine whether the mathematical thinking skills of students diagnosed as gifted differ from their mathematical thinking levels compared to their peers.

## Research questions

Examining the field literature, it is observed that there are limited number of studies that focus on gifted talent specific to the field of mathematics, and limited number of studies showing that the mathematical problem-solving processes of gifted students (Kim et al., 2004; Yıldız et al., 2012) and their mathematical creativity (Haavold, 2013; Taşkın Can, 2013) differ from those of non-gifted students. There are studies on revealing the mathematical thinking processes of the students (Aygün et al., 2020; Baltacı, 2017; Kamarulzaman et al., 2022). In addition, teacher awareness studies on mathematical thinking (Baki and Işık, 2018; Baş, 2013; Coskun et al., 2021; Fisher et al., 2018; Krupa et al., 2017; Lee and Francis, 2018; Nickerson et al., 2017; Superfine et al., 2018; Türker and Yetkin, 2021) and review studies (Akdoğan, 2021) was made. As a result, determining the level of mathematical thinking of gifted students is considered an important issue in terms of revealing the factors behind the success of these students as well as reflecting the

reasons for their failures on the contrary. In this study, unlike other studies, the mathematical thinking levels of gifted and non-gifted students have been discussed comparatively. In addition, the scores of both student groups from the Mathematical Thinking Scale (MTS) will be compared in terms of gender, grade level and mathematics achievement grade variables, and it is thought that the research findings will contribute to the field literature. In this context, this study aimed to determine the mathematical thinking levels of gifted and non-gifted students and to compare them according to some variables (gender, grade level and mathematical achievement). For this purpose, the following research questions were formed:

1. What are the levels of mathematical thinking of gifted and non-gifted students?
2. Do gifted students differ in mathematical thinking levels based on gender, grade level and mathematics achievement?
3. Do the levels of mathematical thinking of non-gifted students differ according to gender, grade level and mathematics achievement?

## METHOD

### Research pattern

In this study, which aims to compare the Mathematical Thinking (MT) levels of gifted (G) and non-gifted (NG) students from 5-8 grade secondary school students in terms of different variables, a screening model from quantitative research methods was used. Screening models are research approaches that aim to depict a past or current situation as it exists (Karasar, 2009).

### Study group

The research was carried out with 194 G students attending SAC from 5-6-7-8 grade students of secondary school in a province located in the southern region of Turkey and 168 NG students studying at the 5-8th grade level of a randomly selected public school from the same province. The fact that students attend SAC means that they are diagnosed as G. The G student group is limited to students who are nominated by their teachers with the observation forms sent to the schools by SAC and who continue to SAC by successfully completing the diagnostic processes. These students, who study at SAC in addition to their formal education, are students whose IQ score is determined to be 130 and above by a standardized test conducted by the Ministry of National Education. Descriptive statistics about the study group of the study are presented in Table 1.

While G students constitute 53.59% of the sample, NG students constitute 46.40%. NG students at all grade levels (43 fifth graders, 40 sixth graders, 50 seventh graders, 35 eighth graders) are evenly distributed. In the distribution of G students (50 fifth graders, 82 sixth graders, 36 seventh graders, 26 eighth graders), there is a decrease in the number of students with the increase in grade level. It can be seen that female students (105 girls, 63 boys) are higher than female students (105 girls, 63 boys) according to gender, while the ratio of male students (85 girls, 109 boys) is higher in the distribution of G students. It is seen that the majority of the students

**Table 1.** Descriptive statistics.

Variable	G		NG	
	N	%	N	%
<b>Gender</b>				
Female	85	43.8	105	62.5
Male	109	56.2	63	37.5
<b>Grade Level</b>				
5	50	25.8	43	26.5
6	82	42.3	40	23.8
7	36	18.6	50	29.8
8	26	13.4	35	20.8
<b>Mathematics course grade</b>				
Low level (3 and lower)	33	17.0	38	22.6
Moderate level (4)	42	21.6	40	23.8
Good level (5)	119	61.3	90	53.6
Total	194	100	168	100

have a mathematics report card grade at the intermediate level and above.

#### Data collection tool and analysis of data

In the study, the Mathematical Thinking Scale (MTS) developed by Er et al. (2023) was used to determine the MT levels of the participants. The sub-factors of the MTS include "Inductive and deductive thinking (7 items)", "Utilitarian thinking (3 items)", "Planned thinking (3 items)", and "Problem-solving based thinking (3 items)". The internal consistency coefficient of the 16-item MTS used in this study was found to be 0.87. The obtained reliability coefficient shows that the scores related to the scale are reliable and can be used for research purposes (Tavşancıl, 2002).

All data of the study were collected by the researcher. The scale took approximately 25 minutes to implement. The mathematics achievements of the students are determined by the grades of the students' mathematics courses in the previous semester, which are registered in the system in their schools. After checking the assumptions of normality of the MTS scores of the students according to the variables and the equality of the variances, it was decided which analyzes would be performed. Kolmogorov Smirnov statistics analytical test values (N and skewness-flatness values) were examined whether the scores obtained from the scale provided normality for each data group. The values of  $\pm 1$ ,  $\pm 1.5$ ,  $\pm 1.96$ ,  $\pm 2$ ,  $\pm 3$ ,  $\pm 3.29$  are proposed for the assumption of normality in the field literature. In this study, the  $\pm 2$  approach (George and Mallery, 2019) was considered in the examination of skewness and flatness values.

Data Analysis of whether the MT levels of the G and NG students showed a statistically significant difference was examined by performing the t-test of unrelated samples. Whether the mean MTS scores of the G and NG students showed a significant difference according to the gender variable was examined by applying ANOVA test or not and whether there was a significant difference according to grade level and mathematics achievement grade variables was examined by applying a single-factor analysis of variance (Ford and Harris, 1992). Scheffetest, one of the complementary post-hoc analysis techniques, was applied to determine between which groups the significant difference found with single-factor ANOVA was found. In this process,  $p = 0.05$  was

accepted for the significance value in the process of analyzing all statistical analyzes.

## FINDINGS

### Comparison of MTS scores of G and NG students

First, it was examined by applying the unrelated groups' t-test, the total score obtained from the MTS scale and the scores obtained from the sub-factors. The results are given in Table 2. Examining Table 2 is examined, there is no statistically significant difference in the mean MTS total scores of G and NG students ( $t(360) = 1.825$ ,  $p > 0.05$ ). MTS averages of NG students ( $\bar{X} = 61.52$ ), are lower than those of G students ( $\bar{X} = 64.10$ ). There is a statistically significant difference in the mean of factor 1 score, which is the sub-factor of the MTS scale of G and NG students. Accordingly, it can be said that the MT levels of G students are higher than those of NG students, but this difference is not significant. In addition, considering that the maximum score that can be taken from the scale is 80, it can be said that the MT levels of the students in both groups are high.

### Comparison of MTS scores of G and NG students by gender

The findings obtained as a result of the t-test are presented in Table 3. Examining Table 3, it was seen that the mean MTS total scores of the G and NG students did not show a statistically significant difference according to the gender variable ( $t(192) = .588$ ,  $t(166) = .276$ ,  $p > 0.05$ ). It was observed that average scores of female students in the G group from MTS ( $\bar{X} = 64.81$ ) were higher than

**Table 2.** Unrelated groups t-test results.

Factors	Groups	N	A.O	Ss	T	Sd	P
F1	G	194	29.38	7.10	2.199	360	0.029*
	NG	168	27.91	5.33			
F2	G	194	11.74	3.66	1.444	360	0.150
	NG	168	11.21	3.30			
F3	G	194	11.41	3.41	1.205	360	0.229
	NG	168	11.00	3.02			
F4	G	194	11.56	3.61	0.463	360	0.644
	NG	168	11.39	3.00			
Total	G	194	64.10	14.69	1.825	360	0.069
	NG	168	61.52	11.72			

**Table 3.** Students' mathematics thinking scale scores by gender.

Students	Gender	N	$\bar{X}$	Ss	T	Sd	P
Gifted	Female	85	64.81	15.12	0.588	192	0.557
	Male	109	63.55	14.40			
NG	Female	105	61.72	11.64	0.276	166	0.783
	Male	63	61.20	11.96			

**Table 4.** Change of students' mts scores by grade level.

Students	Grade	N	$\bar{X}$	Ss		Sum of squares	Sd	Squares Avg.	F	p
G	5	50	67.28	14.24	Ga	8112.341	3	2704.114	15.295	.000
	6	82	56.98	14.23	Gi	33592.386	190	176.802		
	7	36	68.47	13.81	Total	41704.727	193			
	8	26	74.42	4.74						
NG	5	43	63.44	12.05	Ga	311.895	3	103.965	0.753	0.522
	6	40	61.95	12.52	Gi	22653.956	164	138.134		
	7	50	60.88	11.54	Total	22965.851	167			
	8	35	59.62	10.71						

Intergroup: Ga; In-group: Gi

those of male students ( $\bar{X}=63.55$ ), and similarly that average scores of female students in the NG group from MTS ( $\bar{X}=61.72$ ), were higher than those of male students ( $\bar{X}=61.20$ ). Accordingly, it can be said that the MT levels of female students in both groups are higher than those of male students.

#### Comparison of MTS scores of G and NG students according to grade levels

The findings obtained as a result of the ANOVA test are

presented in Table 4. According to Table 4, it was found that the mean scores of G students from MTS showed a significant difference according to their grade level ( $F(3, 194) = 15.295, p < 0.05$ ). Total score averages of the G students participating in the study were as follows respectively from lowest to highest: sixth grade ( $\bar{X}=56.98$ ), fifth grade ( $\bar{X}=67.28$ ), seventh grade ( $\bar{X}=68.47$ ) and eighth grade ( $\bar{X}=74.42$ ). The Scheffe test, one of the multiple comparison tests, was used to determine the direction of the significant difference. According to the analysis results the difference between fifth, seventh and eighth grade G students is in favor of sixth grade students. In

**Table 5.** Change of students' mts scores according to mathematics achievement.

Students	Mathematics achievement	N	$\bar{X}$	Ss		Sum of squares	Sd	Squares Avg.	F	p
G	Low	30	49.60	18.50	Ga	12487.644	2	6243.822	40.818	0.000*
	Moderate	35	56.14	15.46	Gi	29217.083	191	152.969		
	Good	129	69.64	9.33	Total	41704.727	193			
NG	Low	38	56.26	15.14	Ga	2150.619	2	1075.309	8.524	0.000*
	Moderate	40	59.37	9.93	Gi	20815.232	165	126.153		
	Good	90	64.71	9.75	Total	22965.851	167			

addition, it was found that the mean scores of the NG students from MTS did not differ significantly according to the grade level ( $F(3.168) = 0.753, p > .05$ ). Total score averages of the NG students participating in the study were as follows respectively from lowest to highest: eighth grade ( $\bar{X} = 59.62$ ), seventh grade ( $\bar{X} = 60.88$ ), sixth grade ( $\bar{X} = 61.95$ ) and fifth grade ( $\bar{X} = 63.44$ ). Accordingly, it can be said that the level of MT of the G students increases as the grade level increases, while the MT levels of the NG students decrease slightly as the grade level increases.

#### Comparison of MTS scores of G and NG students according to mathematics achievement

The findings obtained as a result of the ANOVA test are presented in Table 5. According to Table 5, it was found that the mean scores of G students from MTS showed a significant difference according to their mathematical achievement ( $F(3.194) = 40.818, p < .05$ ). Total score averages of the G students participating in the study in MTS were as follows from lowest to highest: students with low mathematics achievement ( $\bar{X} = 49.60$ ), students with moderate mathematics achievement ( $\bar{X} = 56.64$ ) and students with good mathematics achievement ( $\bar{X} = 69.64$ ). The Scheffe test, one of the multiple comparison tests, was used to determine the direction of the significant difference. According to the analysis results the difference between G students with moderate mathematics achievement and good mathematics achievement is in favor of students with low mathematics achievement.

In addition, it was found that the mean scores of the NG students from MTS showed a significant difference according to their mathematical achievement ( $F(2.168) = 8.524, p < .05$ ). Total score averages of the NG students participating in the study from MTS were as follows from lowest to highest: students with low mathematics achievement ( $\bar{X} = 56.26$ ), students with moderate mathematics achievement ( $\bar{X} = 59.37$ ) and students with good mathematics achievement ( $\bar{X} = 64.71$ ). The Scheffe test, one of the multiple comparison tests, was used to determine the direction of the significant difference.

According to the analysis results the difference between NG students with moderate mathematics achievement and good mathematics achievement is in favor of students with low mathematics achievement. Accordingly, it can be said that the MT levels of both G and NG students increase as their mathematical achievement levels increase.

#### DISCUSSION

This study, which was conducted to determine whether the MT levels of G and NG students and the average scores they received from the MTS scale differed according to gender, grade level and mathematical achievements, was based on the data obtained from 362 students. In line with the first research question, the average scores of G and NG students from MTS were compared. It was observed that there was a statistically significant difference in the mean scores from Factor 1, which is the sub-factor of the MTS scale, in favor of the G students, and as a result of the comparison of the average scores taken from the whole scale, it was seen that the G students had a higher average than the NG students, but this difference was not significant. Accordingly, it can be said that the MT levels of G students are higher than those of NG students. In addition, considering that the maximum score that can be taken from the scale is 80, it was observed that the MT levels of the students in both groups are high. Gagne (2004) expressed the concept of superior ability as the individual's intelligence age being above normal and performing at a high level in reasoning and abstract thinking skills. Gifted individuals have a high level of sense of duty and creative skills and above-average academic ability (Renzulli, 1978). Gifted individuals are by nature high-level performers in many areas compared to their peers. These research findings are similar to the findings of the field literature.

In line with the second and third research questions, the status of the MTS total score averages of the G and NG students according to the variables (gender, grade level, mathematics course success) was examined. It

was observed that the mean MTS total score of both G students and NG students did not show a statistically significant difference according to gender variable. In addition, it was observed that the MT levels of female students in both groups were higher than male students. Akçakın and Kaya (2020) examined the variation of mathematical thinking styles according to gender in their study. Researchers stated that female students have more analytical thinking style than male students, and male students have more visual thinking style than female students. Gürtaş (2021) examined the mathematical thinking and problem solving skills of secondary school 7th grade students on rational numbers in his study, in which both qualitative and quantitative methods were used. As a result of the research, it was seen that the mathematical thinking and problem solving skills of the students were not at the desired level, and there were statistically significant differences when the participants were examined in terms of variables such as gender, parental education level, the schools they attended, and the reading time. In his study titled "A review on MT skills", Duran (2005) examined the power of some variables related to MT applied to 15-year-old students within the scope of PISA to predict the success of MT skills. As a result of the research, it was reported that male students were more successful than female students, and those who received pre-school education were more successful than those who did not receive pre-school education. In the study titled "Development of MT in Prospective Teachers" by Alkan and Güzel (2005), it was examined that the MT levels of prospective teachers did not constitute a significant difference in terms of gender. Although there is a significant difference in the two sub-factors, it can be said that parallel results have emerged with this research when the whole scale is considered. Him (2006) conducted research on the self-regulatory learning of gifted students in the field literature, and found that male and female students were similar in terms of average scores in terms of intrinsic motivation, test anxiety, cognitive strategy use, and self-regulation, and that the results did not differ significantly. Pajares and Graham (1999) also reached similar conclusions. Accordingly, it can be said that this research finding is similar to the field literature. It was found that the average scores of gifted students from MTS differed significantly according to grade level. However, this does not apply to NG students.

The difference between the average scores of gifted students from the fifth, seventh and eighth grade MTS is in favor of sixth grade students. It was observed that the level of MT of the gifted students increases as the grade level increases, while the MT levels of the NG students decrease slightly as grade level increases. Baş (2019) investigated the relationship between secondary school students' attitudes towards mathematics, mathematical thinking, and problem solving. As a result

of the research, it was seen that the students' attitudes towards all three variables were above the medium level, and these attitudes did not differ according to gender, but differed according to grade level. In addition, it was seen that the average scores of both gifted students and NG students from MTS showed significant differences according to their mathematical success. Accordingly, it can be said that the MT levels of for both groups of students increase as their mathematical achievement levels increase. Tüzün and Cihangir (2020) determined the relationship between the MT stages of secondary school students and their mathematical self-efficacy. The researchers found that there was a positive moderate level relationship between the students' mathematics course final scores and their mathematical self-efficacy and MT stages, as well as between the MT stages and mathematics self-efficacy. In addition, in the field literature, Karakoca (2011) revealed a significant differentiation in the variable of mathematical achievement in MT situations in problem solving. In the study by Alkan and Güzel (2005), it was seen that there was a linear relationship between prospective mathematics teachers' scores from the analysis courses and their level of mathematical thinking. In addition, it was seen that there was a significant relationship between MT and mathematical success in Mubark (2005)'s study, there was a strong relationship between MT and mathematical achievements in Nepal (2016)'s study, and there was a positive significant relationship between MT and success in Kocaman (2017) study. Accordingly, it can be said that this research finding is similar to findings in the field literature.

Consequently, in this research, it has been observed that the MT levels of G students were significantly higher according to their grade level; however, this did not apply to NG students. In addition, it was found that the MT levels of female students were higher than the MT levels of male students in gifted and NG student groups, but this difference was not statistically significant. In addition, it was seen that the success grade of the mathematics course made a significant difference on the level of MT of both the gifted and NG student groups.

## CONCLUSION AND RECOMMENDATION

It is important for individuals to have this skill because they use MT skills in analyzing the events and phenomena they encounter at every stage of life. In his study titled "The effects of MT skills on the academic achievements, problem-solving skills and attitudes of primary school students in technology and science courses", Taşdemir (2008) examined the effects of a unit in technology and science course on attitude, academic achievement, and problem-solving skills of groups that continue constructivist learning and normal education

with teaching that includes constructivist learning-based MT activities. According to the results of the study, it was determined that constructivist-based teaching, which includes MT activities, has a significant effect on the development of students' academic achievements, attitudes and problem-solving skills and on ensuring their continuation. Ayllón et al. (2016) examined the relationship between the development of MT and creativity through mathematical problem posing and solving, and creativity in mathematical problem solving and creation. According to the results of the study, a significant relationship was found. In order for the MT levels of both gifted students and NG students to be at the desired level, it is recommended to design teaching environments that develop this skill and to examine the effectiveness. In addition, in this research, MT levels were discussed and compared with the MT scale. In addition, the mathematical processes of G and NG students in the problem-solving process can be discussed together. In addition, it is recommended to conduct correlation studies in which different ways of thinking such as creative thinking and critical thinking are considered together. It is recommended to include more activities to develop mathematical thinking skills in the mathematics teaching curriculum. In addition, teachers can be given trainings to support the teaching process in gaining mathematical thinking skills. In addition, students', teachers' and pre-service teachers' mathematical thinking skills and processes can be examined.

### Limitations

This study, which was conducted to determine whether the MT levels of gifted and NG students and the average scores they received from the MTS scale differed according to gender, grade level and mathematical achievements, was limited with the data obtained from 362 students. It was assumed that the students sincerely responded to the scale items.

### CONFLICT OF INTERESTS

The author has not declared any conflict of interests.

### REFERENCES

- Akçakın V, Kaya G (2020). Determining mathematical thinking styles of secondary school students: Latent class analysis. *Education and Science*. 45:201.
- Akdogan E (2021). Examination of postgraduate theses written on mathematical thinking and mathematical reasoning in Turkey. Master's Thesis, Eskişehir Osmangazi University, Institute of Educational Sciences, Department of Mathematics and Science Education, Eskişehir.
- Alkan H, Güzel EB (2005). Öğretmen adaylarında matematiksel düşünmenin gelişimi. *Gazi Üniversitesi Gazi Eğitim Fakültesi Dergisi* 25(3):221-236.
- Ataman A (2004). Gifted and gifted children. *Gifted children* pp.158-159.
- Aygün Y, Orbay K, Güç FA (2021). Üstün Yetenekli Tanısı Konulmuş Ve Konulmamış Öğrencilerin Matematiksel Düşünme Süreçlerinin Karşılaştırılması. *Milli Eğitim Dergisi* 50(229):337-362.
- Ayllón MF, Gómez IA, Ballesta-Claver J (2016). Mathematical Thinking and Creativity through Mathematical Problem Posing and Solving. *Journal of Educational Psychology-Propósitos y Representaciones* 4(1):195-218.
- Bakar F, Avan Ç, Aydın B (2018). Üstün yetenekli öğrenciler ve normal akranlarının geri dönüşüm ve çevresel etkileri üzerine tutumlarının karşılaştırılması. *Kastamonu Eğitim Dergisi* 26(3):935-944.
- Baki GÖ, Işık A (2018). Examining teachers' awareness levels of students' mathematical thinking: lesson study model. *Turkish Journal of Computer and Mathematics Education (TURCOMAT)* 9(1):122-146.
- Baltacı A (2017). A Comparison of Syrian Migrant Students in Turkey and Germany: Entrepreneurial Tendencies and Career Expectations. *European Journal of Educational Research* 6(1):15-27.
- Bas S (2013). Examination of teachers' abilities to recognize students' mathematical thinking styles within the framework of a professional development program. Doctoral Thesis, Middle East Technical University, Institute of Science and Technology, Ankara.
- Bas A (2019). Examining the relationship between secondary school students' attitudes towards mathematical thinking, problem solving and mathematics. Master's Thesis, ZonguldakBülentEcevit University, Institute of Science, Department of Mathematics and Science Education, Zonguldak.
- Burton L (1984). Mathematical Thinking: The struggle for meaning. *Journal for Research in Mathematics Education* 15(1):35-49.
- Coskun SD, Sitrava RT, Bostan MI (2021). Pre-service elementary teachers' noticing expertise of students' mathematical thinking: The case of fractions. *International Journal of Mathematical Education in Science and Technology* pp. 1-18.
- Davis G (2006). Gifted children and gifted education: A handbook for teachers and parents.
- Demirtaş B (2018). The relationship between classroom teachers' sensitivity to the phenomenon of creativity and their mathematical thinking skills. [Unpublished master's thesis]. Istanbul University, Cerrahpaşa Graduate Education Institute, Istanbul.
- Duran N (2005). A research on mathematical thinking skills. Unpublished Master's Thesis, Hacettepe University, Social Sciences Institute, Ankara.
- Egan K (1975). How to ask questions that promote high-level thinking. *Peabody Journal of Education* 52(3):228-234.
- Er Z, DinçArtut P, Bal AP (2023). Developing the Mathematical Thinking Scale for Gifted Students. *Pegem Journal of Education and Instruction* 3(3):215-227.
- Fisher MH, Thomas J, Schack EO, Jong C, Tassel J (2018). Noticing numeracy now! Examining changes in preservice teachers' noticing, knowledge, and attitudes. *Mathematics Education Research Journal* 30(2):209-232.
- Ford DY, Harris JJ (1992). The elusive definition of creativity. *The Journal of Creative Behavior*.
- Freudenthal H (1981). Major problems of mathematics education. *Educational Studies in Mathematics* 12:133-150
- Haavold PØ (2013). What are the characteristics of mathematical creativity? An empirical and theoretical investigation of mathematical creativity. Unpublished doctorate dissertation. University of Tromsø, Norway.
- Gagné F (2004). Transforming gifts into talents: The DMGT as a developmental theory. *High Ability Studies* 15(2):119-147.
- Gürtaş K (2021). Ortaokul 7. Sınıf Öğrencilerinin Rasyonel Sayılar Konusundaki Matematiksel Düşünme Ve Problem Çözme Becerilerinin İncelenmesi. *Pearson Journal* 6(15):552-562.
- Henderson PB, Hitchner L, Fritz SJ, Marion B, Scharff C, Hamer J, Riedesel C (2003). Materials development in support of mathematical thinking. *ACM SIGCSE Bulletin* 35(2):185-190.
- Him NM (2006). Self-regulated Learning Strategies of Mathematically Gifted Students, Yüksek Lisans Tezi, The University of Hong Kong Hong Kong.
- Kamarulzaman MH, Kamarudin MF, Sharif MSAM, Esrati MZ, Saali



- MMSN, Yusof R (2022). Impact of Differentiated Instruction on the Mathematical Thinking Processes of Gifted and Talented Students. *Journal of Education and e-Learning Research* 9(4):269-277.
- Karakoca A (2011). Altıncı sınıf öğrencilerinin problem çözmede matematiksel düşünmeyi kullanma durumları (Master's thesis, Eğitim Bilimleri Enstitüsü).
- Karasar N (2009). Bilimsel araştırmaya yöntemleri: Kavramlar-ilkeler-teknikler. Ankara: Nobel Yayın Dağıtım.
- Kim H, Cho S, Ahn D (2004). Development of mathematical creative problem solving ability test for identification of the gifted in math. *Gifted Education International* 18(2):164-174.
- Kocaman M (2017). Investigation of mathematical thinking and the reasoning skills of the 11th grade students. Unpublished Master Thesis]. Balıkesir University, Balıkesir.
- Krupa EE, Huey M, Lesseig K, Casey S, Monson D (2017). Investigating secondary preservice teacher noticing of students' mathematical thinking. In: Schack E, Fisher M, Wilhelm J (eds) *Teacher Noticing: Bridging and Broadening Perspectives, Contexts, and Frameworks*. Research in Mathematics Education pp. 49-72.
- Krutetskii VA (1976). The psychology of mathematical abilities in school children. Chicago, IL: University of Chicago Press.
- Lee MY, Cross FD (2018). Investigating the relationships among elementary teachers' perceptions of the use of students' thinking, their professional noticing skills, and their teaching practices. *The Journal of Mathematical Behavior* 51:118-128.
- Liu PH (2003). Do Teachers Need To Incorporate The History Of Mathematics In Their Teaching? *The Mathematics Teacher* 96(6):416.
- Mason J, Burton L, Stacey K (1985). *Thinking Mathematically*. Revised Edition. England: Addison Wesley Publishers, Wokingham.
- Millî Eğitim Bakanlığı (MEB) (2018). Matematik müfredatı (ilkokul ve ortaokul 1, 2, 3, 4, 5, 6, 7 ve 8. sınıflar). Ankara: MEB, Millî Eğitim Bakanlığı tarafından Ocak 2017'de.
- Mubark MM (2005). Mathematical thinking and mathematics achievement of students in the year 11 scientific stream in Jordan (Yayımlanmamış doktora tezi). Faculty of Education and Arts, University of Newcastle, Avustralya.
- Nepal B (2016). Impact of gender and location on mathematical thinking and mathematics achievement. *Journal of Advanced Academic Research* 3(3):11-21.
- Nickerson SD, Lamb L, LaRochelle R (2017). Challenges in measuring secondary mathematics teachers' professional noticing of students' mathematical thinking. In *Teacher Noticing: Bridging and Broadening Perspectives Contexts and Frameworks* (pp. 381-398). Springer, Cham.
- Pajares F, Graham L (1999). Self-efficacy, motivation constructs, and mathematics performance of entering middle school students. *Contemporary Educational Psychology* 24(2):124-139.
- PISA (Uluslararası Öğrenci Değerlendirme Formu) (2015). "PISA 2015 Ulusal Raporu", [http://pisa.meb.gov.tr/wpcontent/uploads/2016/12/PISA2015\\_Ulus\\_al\\_Rapor1.pdf](http://pisa.meb.gov.tr/wpcontent/uploads/2016/12/PISA2015_Ulus_al_Rapor1.pdf)
- Polya G (1945). *How to solve it*, Princeton. NJ: Princeton U. Press.
- Renzulli JS (1978). What makes giftedness? Reexamining a definition. *Phi Delta Kappan* 60(3):180.
- Schoenfeld AH (1992). Learning to think mathematically: Problem solving, metacognition and sense-making in mathematics. D. Grouws (Ed.), *Handbook for research on mathematics teaching and learning* (s. 334-370) içinde. New York: MacMillan.
- Sontay G, Gökdere M, Usta E (2014). A Comparative Investigation of Environmental Behaviors of Gifted Students and Their Peers/Üstün Yetenekli Öğrencilerle Akranlarının Çevresel Davranışlarının Karşılaştırmalı İncelenmesi. *Türk Üstün Zekâve Eğitim Dergisi* 4(2):90-106.
- Superfine A, Amador J, Bragelman J (2018). Facilitating video-based discussions to support prospective teacher noticing. *The Journal of Mathematical Behavior* 54:100681.
- Tall D (1991). *Advanced Mathematical Thinking*, New York, Kluwer.
- Tall D (2002). *Advanced Mathematical Thinking*. USA: Kluwer Academic Publishers.
- Taşdemir A (2008). Matematiksel düşünme becerilerinin ilköğretim öğrencilerinin fen ve teknoloji dersindeki akademik başarıları, problem çözme becerileri ve tutumları üzerine etkileri. *Gazi Üniversitesi, Ankara*.
- Taşkın Can B (2013). The Effects of Using Creative Drama in Science Education on Students' Achievements and Scientific Process Skills. *İlköğretim Online* 12(1).
- Tavşancıl E (2002). *Tutumların Ölçülmesi ve SPSS ile Veri Analizi*. Ankara: Nobel Yayınları.
- Tuncay HA (2015). *Matematiksel düşünme süreçlerinin incelenmesi*. (Yüksek Lisans Tezi). <https://tez.yok.gov.tr> sayfasından erişilmiştir.
- Türker BB, Yetkin Ö (2021). Matematiksel Modelleme Etkinlikleri Bağlamında Öğrenci Düşüncelerine Yönelik Öğretmen Farkındalığı ve Fark Etme Stratejileri. *Pamukkale Üniversitesi Eğitim Fakültesi Dergisi* (53):521-554.
- Tüzün M, Cihangir A (2020). Ortaokul Öğrencilerinin Matematiksel Düşünme Aşamaları ile Matematik Öz Yeterlilikleri Arasındaki İlişkinin İncelenmesi. *Ahmet Keleşoğlu Eğitim Fakültesi Dergisi* 2(2):210-228.
- Yenilmez K (2007). İlköğretim Matematik Öğrencilerinin Matematik Dersine Yönelik Tutumlar, Ondokuz Mayıs Üniversitesi Eğitim Fakültesi Dergisi 2(3):51-59.
- Yeşildere S (2006). Farklı matematiksel güce sahip ilköğretim 6, 7 ve 8 sınıf öğrencilerinin matematiksel düşünme ve bilgiyi oluşturmasındaki süreçlerini incelenmesi. Doctoral dissertation, DEÜ Eğitim Bilimleri Enstitüsü.
- Yıldız A, Baltacı S, Kurak Y, Güven B (2012). Examining the usage of problem-solving strategies by the eighth grade gifted and non-gifted students. *Journal of Uludağ University Faculty of Education* 25(1):123-143.