

*Full Length Research Paper*

# **Monitoring the loss of mass or the volume recessed into a waveguide by resonant signal principle: Nano-inscribed slots in DUV210 micro-resonators**

**Arthur Doliveira<sup>1</sup>, Lucas Garnier<sup>2</sup>, Fabrice Mahé<sup>1</sup>, Hervé Lhermite<sup>2</sup>, Etienne Gaviot<sup>3</sup> and Bruno Bêche<sup>2\*</sup>**

<sup>1</sup>Institut de Recherche Mathématique de Rennes, Université de Rennes, 6625, F-35000 Rennes, France.

<sup>2</sup>Institut d'Électronique et des Technologies du numÉriques, Université de Rennes, 6164, F-35000 Rennes, France.

<sup>3</sup>Laboratoire d'Acoustique de l'Université du Maine, Université du Maine, 6613, F-72000 Le Mans, France.

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**The goal of this paper is to study the impact of a differential mass loss or a lack of material (void) directly located into the core structure of matter together with the possibility of measuring its effect by a resonant signal surface at optical frequencies. To this end, the focus has been on the evolution of effective indices or eigenvalues of micro-resonators as relevant models. Specific lack of mass was measured by way of a resonant optical signal principle. Then, specific families of resonators have been designed and shaped with several slits nano-inscribed upon them. The signal resonant light is then characterized by its pseudo-period while considering the whole geometry, taking account of the void; thus, it contains the information regarding the pre-defined recessed volume. The study was carried out first by controlling the deep UV technology onto an organic so as to fabricate the family of slotted micro-resonators before assessing the evolution of the effective index of the system that is inversely proportional to the free spectral range. Experimentally, the design of the measurement platform made it possible to measure the impact of a given lack of material within the cyclic resonators. Experimental measurements have been carried out so as to confirm previous simulations demonstrating a convergence ranging from 0.09 to 0.39%. Accordingly, the relevant results allow us to validate a quantified description regarding the hollowed out volume (or mass recessed within the core waveguide) with regard to the spatial resonant optical signal.**

**Key words:** Deep UV210 polymer, nano-inscribed slots, micro-resonators, optical resonance monitoring, lack of material, void characterizations.

## **INTRODUCTION**

Historically and then currently on the market, integrated devices measuring or detecting differential variations in

micro-mass are based on the propagation of tunable piezo-elastic or acoustoelectric waves (bulk acoustic

wave, BAW and surface acoustic wave, SAW) (Royer and Dieulesaint, 1999). The principle may be reduced to an equivalent piezoelectric resonator structure that is shifted in tune (Benetti et al., 2005). In such piezo-elastic physics, the general resolution amounts to solving a problem of eigenvalues (velocity of the acoustic wave into the solid) and eigenvectors (displacements and associated stress) (Farnell, 1970; Fahmy and Adler, 1973). Nowadays and over the past two decades, integrated photonics based on optical micro-resonators has been developed with different materials and processes (Rabus, 2007; Monte et al., 2010; Isci et al., 2004). The latter are mainly defined by a looping back of the optical wave on itself by way of 2D or 3D geometries (Scheuer and Yariv, 2006; Zebda et al., 2008; Delezoide et al., 2012; Sanogo et al., 2013; Pluchon et al., 2013) entailing then a quantization of the modes characterizing the resonant mechanisms. One could wonder about an analogy or approach to be considered between these devices, even if obviously their physics is based on waves of different nature. In the case of a quartz crystal microbalance, resonance wavelengths are shifted by a small addition or removal of mass, and are related to the viscoelastic properties of the sample, whereas in the case of photonic micro resonators, resonance shifts are related to the optical properties of the studied sample. In a recent study, we were able to dynamically follow the evaporation of matter located in contact and therefore above a resonant source of electromagnetic signal (Garnier et al., 2020). In such a case, the differential mass loss or lack of matter (water evaporation) was probed by investigating the evanescent tail and part of the global mode. Such a previous dynamic differential mass process may be considered as an upper cladding disappearing from the photonic resonant structure and can also be compared with the detection of its evaporation on a quartz balance. The extension of this parallel and further study concerns the case regarding the differential lack of matter reaching the guiding part or core of the structure (namely recessed of volume of matter inscribed directly into the guide), still with a resonant probe and same principle. Then, following the study of a differential mass loss clearly established in the part of the evanescent tail of the mode, we aim at studying the entailed behavior when such a loss of mass (or less matter) reaches directly the inner core of the eigenmode. In recent years, concerning the morphology of structures with air nanogap inscribed in the core of the guide, guiding structures have been developed incorporating subwavelength air slits. In particular, Almeida et al. (2004) and Xu et al. (2004) proposed such

designs to obtain a class of specific modes with a strong localization of energy in the air gap featuring the lowest optical index of the layers constituting the complete structure. This paved the way for the production of structures arranged on silicon-based semiconductors (Barios, 2006; Lo et al., 2004; Eti and Kurt, 2016; Campopiano et al., 2004; Chao et al., 2006), particularly fitted to the incorporation of air nano-gaps owing to their technological manufacturing processes. In order to create nano-slits within the core of the structure to model the loss of intrinsic matter, we investigated a polymer called resin UV210 to be flashed in deep UV and its associated lithography processes allowing an apt shaping of such nanogaps or air recessed volumes (Duval et al., 2010; <https://kayakuam.com/products/uv-210gs-positive-duv-photos Resist/>).

The aim of this work is then to study a given evolution of a lack of material that models a given mass loss (medium distributed in air slits) within the core of an optical waveguide (or hollow waveguide), and its impact on resonance, considering its pseudo-period.

## Context and basis with photonics

Concerning the physics of this problem with eigen-vector and -values, let us introduce the basics of resonant electromagnetism. At first, in guided electromagnetism (Collin, 1991) and integrated photonics (Adams, 1981; Snyder and Love, 2000), the calculation of the solutions regarding the propagation equations modes (upstream of the equations of J. C. Maxwell) may be summed up as a problem with eigenvalues and eigenvectors to be solved. When classes of solutions exist mathematically (guided modes, leaky modes, and radiated modes) their relevant eigenvalues stand for effective propagations constants  $\beta = k_0 \cdot n_{\text{eff}}^{\text{phase}} = (2\pi/\lambda_0) \cdot n_{\text{eff}}^{\text{phase}}$  (related to the fixed wave vector  $k_0$  and the fixed wavelength  $\lambda_0$  in wave physics) or their effectives phase indices  $n_{\text{eff}}^{\text{phase}}$  considering the light in the whole system or the overall photonic structure at a fixed wavelength (Bêche and Gaviot, 2016). Such eigenvalues are solutions of opto-geometric equations called eigenvalue equations; each eigenvalue may be associated with a mode unfolded in the complete structure, whose modulus stands for the optical intensity and its specific spatial distribution (Bêche et al., 2010). In a micro-resonator configuration, the cyclical and re-looped quantification is naturally highlighted through the relation  $L_{\text{opt}} = m \cdot \lambda_m$ , with  $L_{\text{opt}} = n_{\text{eff}}^{\text{phase}} \cdot L_{\text{geo}}$  considering the

\*Corresponding author. E-mail: bruno.beche@univ-rennes1.fr

optical/geometrical lengths (or optical/geometrical perimeters) of the specific micro-resonator ( $m$  is an integer and  $\lambda_m$  the successive resonant wavelengths). Only some specific wavelengths  $\lambda_m$  will satisfy successively this perimeter phase matching relationship. In the following, the resonances with a broad spectrum source were tested and therefore have access to the effective group index  $n_{eff}^{group}$  of the considered structures; then the eigenvalue of the whole system which is probed by way of several wavelengths at the same time can

$$\left\{ \begin{array}{l} d\phi(k) = \frac{\partial \phi}{\partial k} \cdot dk = [n_{eff}^{group} \cdot L_{geo}] \cdot dk = 2\pi \\ \text{with, } n_{eff}^{group} = \left[ n_{eff}^{phase}(k_{0,m}) + k_{0,m} \cdot \frac{\partial n_{eff}^{phase}(k_{0,m})}{\partial k} \right] \text{ and } dk = k_{m+1} - k_m \end{array} \right. \quad (2)$$

Such an effective group index  $n_{eff}^{group}$  is markedly higher than the effective phase index  $n_{eff}^{phase}$  of the structure at a fixed wavelength because two dispersive contributions are superimposed; at first the physical dispersion of the UV210 material (representing by  $n_{UV210}^{group}$ ) plus the modal dispersion contribution that is specific with the non-linear dispersion curves of the overall resonant structure; then one can acknowledge the notion of effective index or eigenvalue of the electromagnetic circuit (that as such may be either related to the phase or to the group depending on whether one has considered the indices of phase or of group for all the materials). Thus, experimentally or by simulations in optics, if you operate with a tunable source so as to probe an optical property (such as the resonances) then the system will present its so-called phase response; on the other hand, the use of a wide-spectrum laser source, simultaneously probing the circuit with all the wavelengths, will present a group response because such a light have previously revealed the notion of the group index of materials.

In order to determine a lack of matter or recessed volume by a resonant principle, a suitable purpose to be put forth is therefore to use slot-waveguides (re-looped in micro-resonators structures) so as to measure the evolution of the eigenvalue while assessing the free spectral range:

$$FSR^{(group \text{ or } phase)} = \frac{\lambda_0^2}{n_{eff}^{group \text{ or } phase} \cdot L_{geo}} \quad (3)$$

The intrinsic loss of mass located within the core guiding (air recessed volume fixed by the nano-slits) will bring about a displacement on the curves of dispersion of the eigenvalue. In this study, a broad spectrum source was used: then, relation (3) will be validated with the eigenvalue  $n_{eff}^{group}$ . Such an effective group index  $n_{eff}^{group}$  takes account respectively of all the dispersions including those of the effective eigenvalue equation regarding all

respectively be represented by  $n_{eff}^{group}$ . Resonance is obtained when the light returns to the starting point in phase:

$$\phi(k) = 2\pi \cdot m = k_{0,m} \cdot L_{opt} = k_{0,m} \cdot n_{eff}^{phase} \cdot L_{geo} = \beta_m \cdot L_{geo} \quad (1)$$

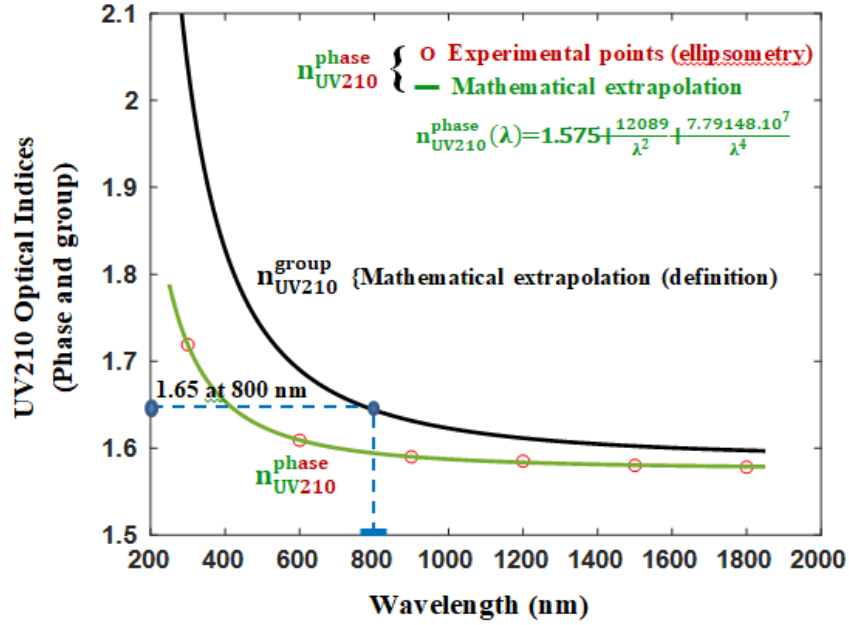
A 1<sup>st</sup> order expansion of Taylor of  $\phi(k)$  gives:

the opto-geometry of the structure.

In addition, so as to be able to compare the simulations with our measurements, it is first necessary to estimate the group index of the UV210 material used to shape the nano-slits. Figure 1 represents the dispersion curves of the UV210 material: ellipsometric measurements (Uvisel, Jobin Yvon-Horiba) were carried out in the range of 300 to 1800 nm so as to determine the dispersion of the optical phase indices  $n_{UV210}^{phase}$  of the material and to deduce the mathematical extrapolation  $n_{UV210}^{phase}(\lambda) = 1.575 + \frac{12089}{\lambda^2} + \frac{7.79148 \cdot 10^7}{\lambda^4}$  (Cauchy's law). The extrapolation of the  $n_{UV210}^{group}$  group index regarding the UV210 material is then obtained directly by the classical optical definition related to  $n_{UV210}^{phase}(\lambda)$  with a gradient. Therefore, the simulations take advantage of such a plot (in black, Figure 1), given that the resonance measurements are carried out experimentally by a broadband laser source. Thus, the value retained for the simulations has been  $n_{UV210}^{group} = 1.65$  around  $\lambda_0 = 800$  nm.

### Simulations

Electromagnetic simulations were driven with a view to estimating the proportion or percentage defining the included lack of matter (or inscribed nano-slits) within a cyclic resonator considering the impact on the eigenvalue  $n_{eff}^{group}$ : then through the parameter  $FSR^{group}$  (Equation 3), one can assess the minimum value to be detectable on a statistic of spectral measurements. Simulations have been carried out by way of the COMSOL Multiphysics software (<https://www.comsol.com/comsol-multiphysics>), as a most efficient solving technique based on the finite element method. Figure 2 represents the geometries of the structures that are modeled prior their associated



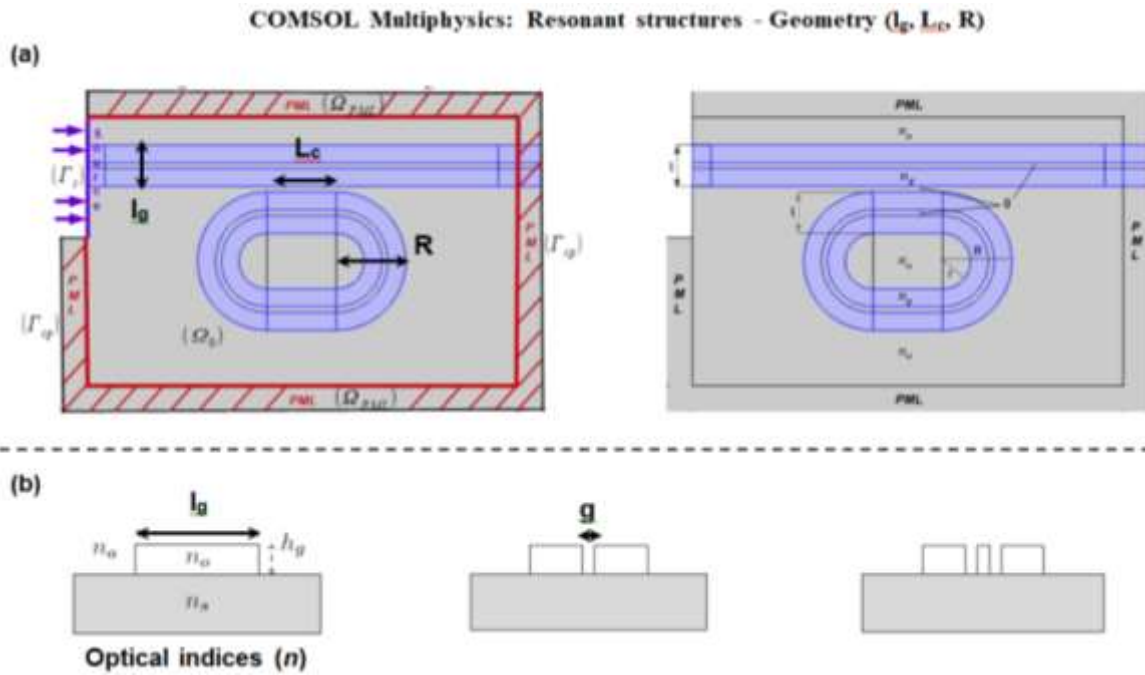
**Figure 1.** Dispersion curves of the UV210 material: optical phase index  $n_{UV210}^{phase}$  of the material measured by ellipsometry plus mathematical extrapolation; the result of Cauchy's law is then estimated as  $n_{UV210}^{phase}(\lambda) = 1.575 + \frac{12089}{\lambda^2} + \frac{7.79148 \cdot 10^7}{\lambda^4}$ . The extrapolation of the group index of the UV210 material  $n_{UV210}^{group}$  is obtained by the classical optical definition that links  $n_{UV210}^{phase}(\lambda)$  with a gradient.

realizations (top view and cross-sectional view). All the opto-geometrical parameters are depicted and detailed in Figure 2, with dimensions (width, height, lengths, radius of curvature plus various optical indices). Since the spectral quantity  $FSR^{group} (\propto 1/n_{eff}^{group})$  is directly proportional to the inverse of the effective group index (Equation 3), a first direct simulation method (I\_2D) have been achieved with regard to the initial condition value of UV210 group index  $n_{UV210}^{group} = 1.65$  at a wavelength 800 nm. Cross-sectional structures are considered in 2D, as depicted in Figure 2b, so as to calculate the eigenvalue  $n_{eff}^{group}$  attached to the guided mode presenting naturally the highest effective group index close to that of the material making up the core waveguide); here, the related waveguides are single-mode (quasi-TE<sub>00</sub>) at the simulation wavelength taken  $\lambda_0 = 800$  nm. Then, considering a compact domain  $\Omega$ , in the present case, the finite element method (COMSOL) allows us to solve the following partial differential problem: (find  $\vec{E} \in [H^2(\mathbb{R}^2)]^3$ ), with given boundary conditions on a distant  $\partial\Omega$  (with  $\vec{u}$  outer normal at the border  $\partial\Omega$ ,  $k_0$  the

wave vector module and  $n$  the index):

$$\begin{cases} \overline{\text{rot rot } \vec{E}} - k_0^2 n^2 = 0, & (\text{into } \Omega) \\ \vec{E} \wedge \vec{u} = 0, & (\text{on } \partial\Omega) \end{cases} \quad (4)$$

Considering the open domain  $\Omega$ ,  $H$  is the Sobolev space; then,  $H^2(\Omega)$  stands for the set of integrable square functions whose second order derivatives feature also integrable square values. Figure 2b displays the relevant schematic diagrams (as cross-sectional views) for the three families of rib-waveguides structures, respectively fitted with none, one and two nano-inscribed slots. Such structures represent the future room devices that will be produced by way of clean room processes. Such rib-waveguides are 3  $\mu\text{m}$  wide ( $l_g$ ), 1  $\mu\text{m}$  thick ( $h_g$ ) and feature a common 400 nm width ( $g$ ) for each nano-slot. Considering the 800 nm wavelength, the optical indices of the materials were fixed with the following values as regard simulations:  $n_a = 1.00$  (air, upper-cladding),  $n_o = 1.65 = n_{UV210}^{group}$  (polymer UV210, core waveguide) and  $n_s = 1.45$  (Silica, lower-cladding). Then the eigenvectors calculations can be achieved, featuring the effective



**Figure 2.** COMSOL Multiphysics: Geometry of the resonant structures. (a) Upper-view of the resonant structures. Such racetrack micro-resonators (MRs) present a radius of curvature  $R = 5 \mu\text{m}$  and a  $5 \mu\text{m}$  coupling length,  $L_c$ : Both waveguides have a same width  $l_g = 3 \mu\text{m}$  (MR with one slot in such example). Beyond the structure,  $\Omega_{\text{PML}}$  represents an area called ‘Perfectly Matched Layer’ avoiding untoward reflections for simulations. The indices of the structure for the study in propagation and spectral resonances will be fixed to the values of the effective indices of the structures; (b) Schematic diagram of the cross-sectional view of the three family waveguides structures respectively made of a rib with no slot and ribs with 1 and 2\_ slots nano-inscribed. At a wavelength of  $\lambda_{00} = 800 \text{ nm}$ , optical indices of the materials are fixed for the simulations at  $n_a = 1.00$  (air, upper-cladding),  $n_o = 1.65$  (group index of the polymer UV210, core waveguide) and  $n_s = 1.45$  (Silica, lower-cladding). The other parameters describe the geometric dimensions with:  $l_g = 3 \mu\text{m}$  as the width of the global rib waveguide, its thickness  $h_g = 1 \mu\text{m}$ , and  $g = 400 \text{ nm}$  the common width of each nano-slot.

index into the light cone (spatial distributions of the single mode quasi-TE) together with the eigenvalues  $n_{\text{eff}}^{\text{group}}$  associated to each family of waveguides (with respectively 0, 1 and 2 inscribed nano-slots) as depicted in Figure 3. With this central cyclic and geometric resonant principle, group effective indices are inversely proportional to the aforementioned FSR parameter ( $\text{FSR}^{\text{group}} \propto 1/n_{\text{eff}}^{\text{group}}$ ).

Thus, with the highest studied dynamic considering no slot and two nano-slots, the relevant COMSOL simulations provide the quantity  $(\text{FSR}_{2\text{slots}}^{\text{group}}/\text{FSR}_{0\text{slot}}^{\text{group}}) = (n_{\text{eff}_0\text{slot}}^{\text{group}}/n_{\text{eff}_2\text{slots}}^{\text{group}}) = (1.6028/1.5714)$ , evaluated at 1.019 (Table 1, simulation I\_2D). Moreover, by way of Equation 3 with  $L_{\text{geo}}=41.5 \mu\text{m}$  (MR described in Figure 5) and  $\lambda_0=800 \text{ nm}$ , it is also possible to estimate  $(\text{FSR}_{2\text{slots}}^{\text{group}} - \text{FSR}_{0\text{slot}}^{\text{group}}) = \frac{\lambda_0^2}{L_{\text{geo}}} \left( \frac{1}{n_{\text{eff}_2\text{slots}}^{\text{group}}} - \frac{1}{n_{\text{eff}_0\text{slot}}^{\text{group}}} \right) = 0.19 \text{ nm}$  (Table 1, simulation I\_2D). Due to the specific

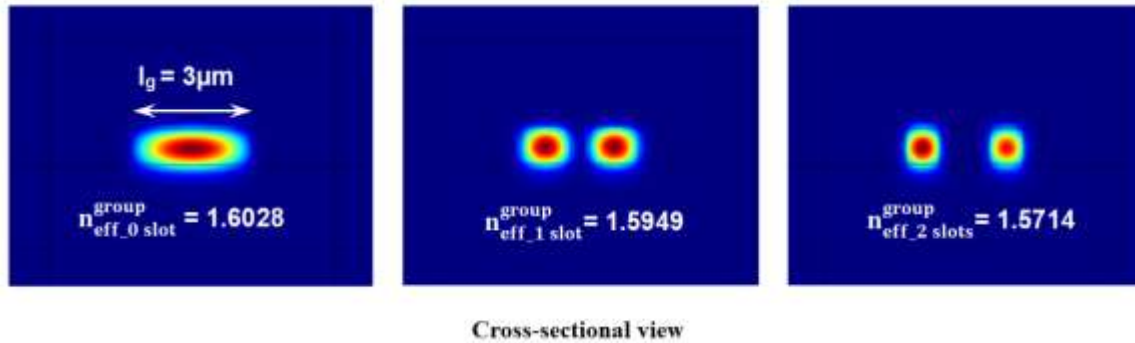
dependence of the parameter  $\text{FSR}^{\text{group}}$ , previously defined, which is inversely proportional to the eigenvalue, the first simulations in two dimensions (I\_2D) thus appear to be an educational and simple first step estimate.

On the other hand, a second and final-simulation II\_3D approach with COMSOL was initiated by a propagation method covering the whole studied structures (complete guides/micro-resonators). Such simulations are intended to investigate the propagation, the coupling and then the resonances for various successive wavelengths  $\lambda_m$  so as to first find optimal conditions and directly assess the relevant  $\text{FSR}^{\text{group}}$  spectral quantities by outlining the global theoretical spectral responses. Figure 4 shows the type of complete structures simulated in the full  $\Omega$  domain  $= \Omega_0 \cup \Omega_{\text{PML}}$ , with  $\Omega_{\text{PML}}$  an ideal layer called Perfectly Matched (absorbent) Layer. The purpose of PML layers is to change the operator of the system in the layer to force the solution to decay inside such a PML layer who belongs to the  $\Omega$  domain. The solution being zero on the edge, we have moreover imposed such a condition of



COMSOL Multiphysics: Simulations I – group effective indices calculations (2D)

Quasi-TE single-mode distribution



**Figure 3.** COMSOL Multiphysics: Simulations I<sub>2D</sub>; COMSOL simulations: calculations of the eigenvectors (spatial distributions of the single mode quasi-TE) plus the eigenvalues as the so-called effective group indices  $n_{eff}^{group}$  associated to each family of waveguides with respectively; 0, 1 and 2 inscribed nano-slots. With such a cyclic and geometric resonant principle, effective indices are inversely proportional to the above-mentioned FSR measurements ( $n_{eff}^{group} \propto 1/FSR^{group}$ , see equation (3)).

**Table 1.** Comparison regarding relative ( $FSR_{2slots}^{group}/FSR_{0slot}^{group}$ ) and absolute average ( $FSR_{2slots}^{group} - FSR_{0slot}^{group}$ ) values linked to the principle of resonance for monitoring a loss of material (the polymer substance) within a resonator (inscription of air nano-gap): comparison between COMSOL modeling I<sub>2D</sub> and II<sub>3D</sub> and the experimental method.

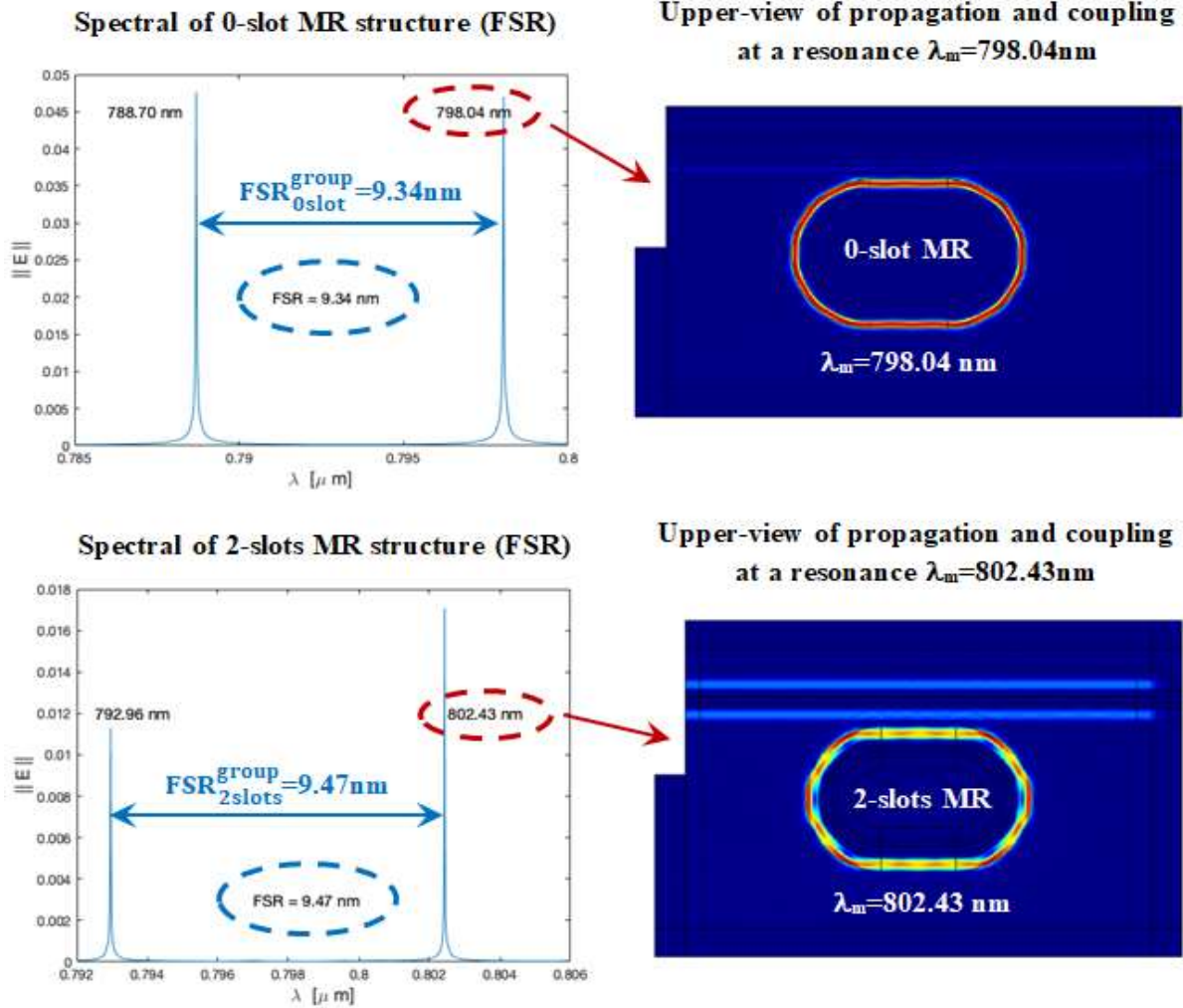
Method	Simulations I <sub>2D</sub>	Simulations II <sub>3D</sub>	Experimental
$(FSR_{2slots}^{group}/FSR_{0slot}^{group})$	1.019 = (1.6028/1.5714)	1.014 = (9.47/9.34)	1.015
$(FSR_{2slots}^{group} - FSR_{0slot}^{group})$	0.19 nm	0.13 nm	0.16 nm

For the simulation I<sub>2D</sub> the average of  $(FSR_{2slots}^{group} - FSR_{0slot}^{group})$  was calculated with a wavelength  $\lambda = 800$  nm and the perimeter  $L_{geo} = 41.5 \mu m$  of the MRs (Figure 5), using equation (3). The impact of the lack of material with the optical surface resonance principle results in a same increase in the relative ratio ( $FSR_{2slots}^{group}/FSR_{0slot}^{group}$ ) on the measurement range (experiment compared to simulations). Deviations from the ratio ( $FSR_{2slots}^{group}/FSR_{0slot}^{group}$ ) measured by experimental method and simulations I<sub>2D</sub> and II<sub>3D</sub> are respectively close to 0.39 and 0.09%.

perfect electrical conductor which corresponds to a homogeneous Dirichlet condition at the border/limit  $\partial\Omega$  of the domain; this condition is fitted with the formulation in electric fields of the Maxwell system. Taking advantage of the second equation of the system (Equation 4), this perfect conductor condition is additionally applied on the boundary denoted  $\Gamma_{cp}$  as depicted in Figure 1a. Globally, this enables to ‘digitally’ avoid any untoward reflection due to the electromagnetic modes at the interface of said layer (or to prevent edge effects). The regions making up the access guide and the micro-resonator fitted with slits have  $n_{eff}^{group}$  as effective group indices (Figure 3), considering guided mode of the light cone; this specific field  $\vec{E}$  acts as the source on  $\Gamma_s$ , triggering off the

propagation, the coupling entailing then potential generated resonances at specific wavelengths. In fact, for successive given wavelengths close to a laser  $\lambda_0 = 800$  nm, the amplitude of the field  $\vec{E}$  in resonance into the looped or resonator part is considered. The rest of the domain consists of ambient air, the other geometric parameters of the structures being those previously defined in Figure 2a. Figure 4 summarizes the determination of each resonance value within a spectral range, entailing  $FSR^{group}$  values for both the 0-slot and the 2-slot structures. In addition, both electromagnetic propagation maps, together with their associated wavelengths regarding coupling and resonance mechanisms are depicted in Figure 4. Such a specific set

COMSOL Multiphysics: Simulations II – propagation and resonances (3D)



**Figure 4.** COMSOL Multiphysics: Simulations II<sub>3D</sub>; geometry and parameters previously defined in Figure 2 (a). COMSOL simulations: determination of each spectral resonance (entailing  $FSR^{group}$  values) for the 0-slot and the 2-slot structures so as to evaluate the global ranging effect of mass recessing (nano-gap of air) within the studied structures.

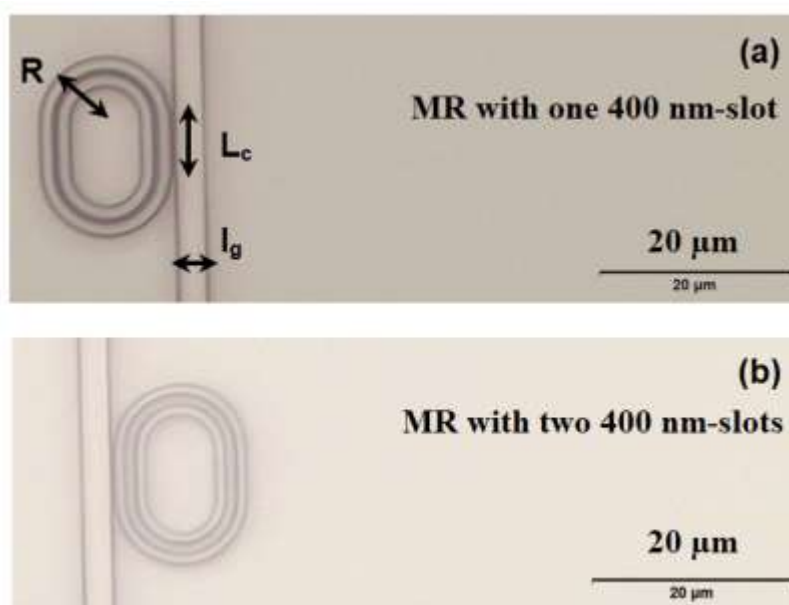
of simulations, based on the propagation/coupling/resonance in the whole domain address the aforementioned structures defined in Figure 2. Then it yields a dynamic on the quantity  $(FSR_{2slots}^{group}/FSR_{0slot}^{group}) = (9.47 / 9.34)$  evaluated at 1.014 (Table 1, simulation II<sub>3D</sub>) with a 26% recessed volume (lack of material considering no slot and 2 slots configurations). According to Table 1, deviations from the ratio  $(FSR_{2slots}^{group}/FSR_{0slot}^{group})$  measured both by experimental method and simulations I<sub>2D</sub> and II<sub>3D</sub> are respectively close to 0.39 and 0.09%. Obviously for the simulation II<sub>3D</sub> the difference  $(FSR_{2slots}^{group} - FSR_{0slot}^{group})=0.13\text{ nm}$  is immediate. Then in such

principle, it seems therefore possible to detect experimentally a given lack of matter with such a weak variation pertaining to resonant electromagnetism.

**FABRICATION OF STRUCTURES AND PROTOCOL MEASUREMENTS**

**Materials and processes**

Here, we describe specific thin film processes developed with the UV210 polymer (with its suited photolithography at 248 nm) for fabricating the so-called resonant



**Figure 5.** Upper-view (optical imaging: magnification  $\times 50$ ) of photonic micro-resonators with inscribed nano-slots featuring a 400 nm fixed width. Such racetrack micro-resonators (MRs) present a radius of curvature  $R = 5 \mu\text{m}$  and a  $5 \mu\text{m}$  coupling length,  $L_c$ : Both waveguides have a same width  $l_g = 3 \mu\text{m}$ . (a) MR with one slot, (b) MR with two slots. In such MR configurations, perimeter  $L_{\text{geo}} = 41.5 \mu\text{m}$ .

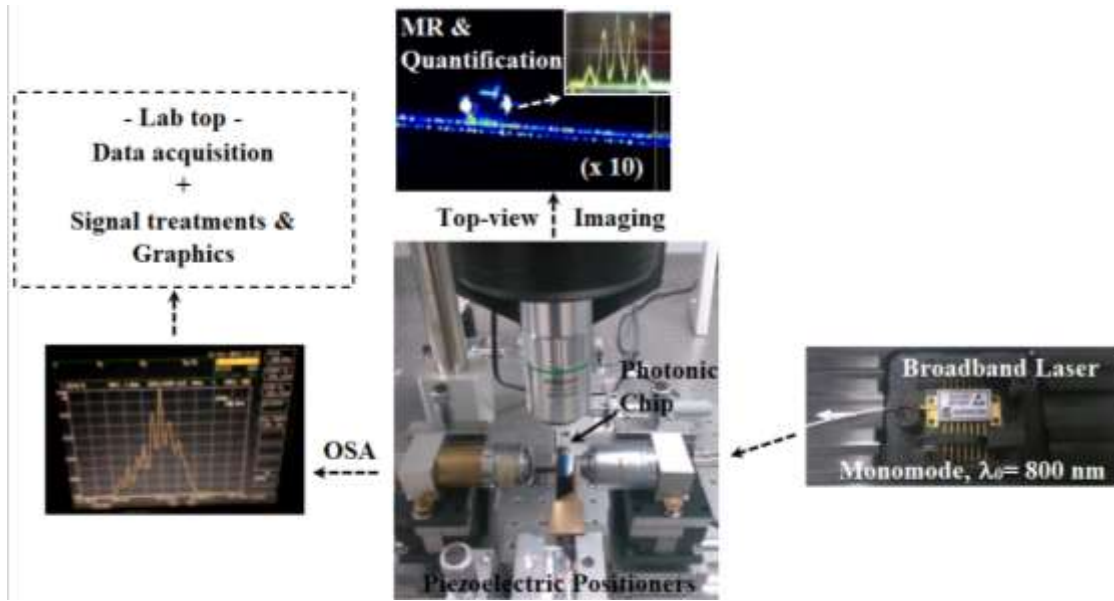
structures with inscribed nano-slits. For the purpose of designing the optical lower cladding, as part of the manufacturing processes, a  $1.5 \mu\text{m}$  thick layer of silica was first produced by thermal oxidation of a 3 inches silicon wafer. Then we used the so called UV210 polymer positive resin, to be exposed in deep UV at 248 nm by a mercury lamp (HBO 1000W/D, OSRAM), and spread by spin-coating, taking advantage of a UV mask aligner (Suss Microtec MA6) for shaping the core waveguide. The UV210 polymer made up of poly (p-hydroxystyrene) and poly (t-butyl acrylate) is a chemically amplified resin. A photo-acid generator is added to the matrix of the copolymer in order to increase the sensitivity of the resin. Low radiation doses are quite suitable to obtain an excellent resolution in the transposed patterns as exposed areas become soluble in a developer such as tetra-methyl ammonium hydroxide (Microposit MF CD-26). They involve namely a deposit/coating prior to a first annealing, a DUV exposure, followed with a second annealing and appropriate development (Table 2). After final curing in the oven (to harden the overall structure and remove all traces of solvent), the polymer proved to afford adequate transparent waveguides at visible and infrared wavelengths. Three families of structures have been produced with respectively no nano-slit, then one, then two, each one featuring a fixed 400 nm width. Figure 5a and b shows an optical imaging of the racetrack

resonators respectively with one (a) and two slots (b) as recessed volumes. Associated waveguides are  $3 \mu\text{m}$  in width ( $l_g$ ). Considering such hollow structures, inscriptions of one or two 400-nm-wide slits entail relevant void volumes with respective percentages of 13% (corresponding of  $16.55 \mu\text{m}^3$ ) and 26% ( $33.1 \mu\text{m}^3$ ). As shown in Figure 5, the other dimension characterizing the resonator is  $R = L_c = 5 \mu\text{m}$  for both the radius and the coupling length leading to the perimeter  $L_{\text{geo}} = 41.5 \mu\text{m}$ .

### Technical protocol of measurements

The chips have been tested within a specific platform in order to assess the  $\text{FSR}^{\text{group}}$  values as functions of the eigenvalues (or effective group indices as mentioned previously in Equation 3), attached to the three types of structures (respectively with none, one or two slots). Figure 6 describes the specific parts of the test platform dedicated to the different tasks and protocols. First of all, the injection is carried out by using a single mode fiber and broadband laser source (SUPERLUM,  $\lambda_{0\text{-center}} = 800 \text{ nm}$ ) with a 40-nm-wide Gaussian spectrum (photograph, Figure 6, bottom right). It is important to realize that it is the effective group index defined in Equation 3 that must be taken into account in the  $\text{FSR}^{\text{group}}$  resonant parameter because the structure is activated by a broad-spectrum





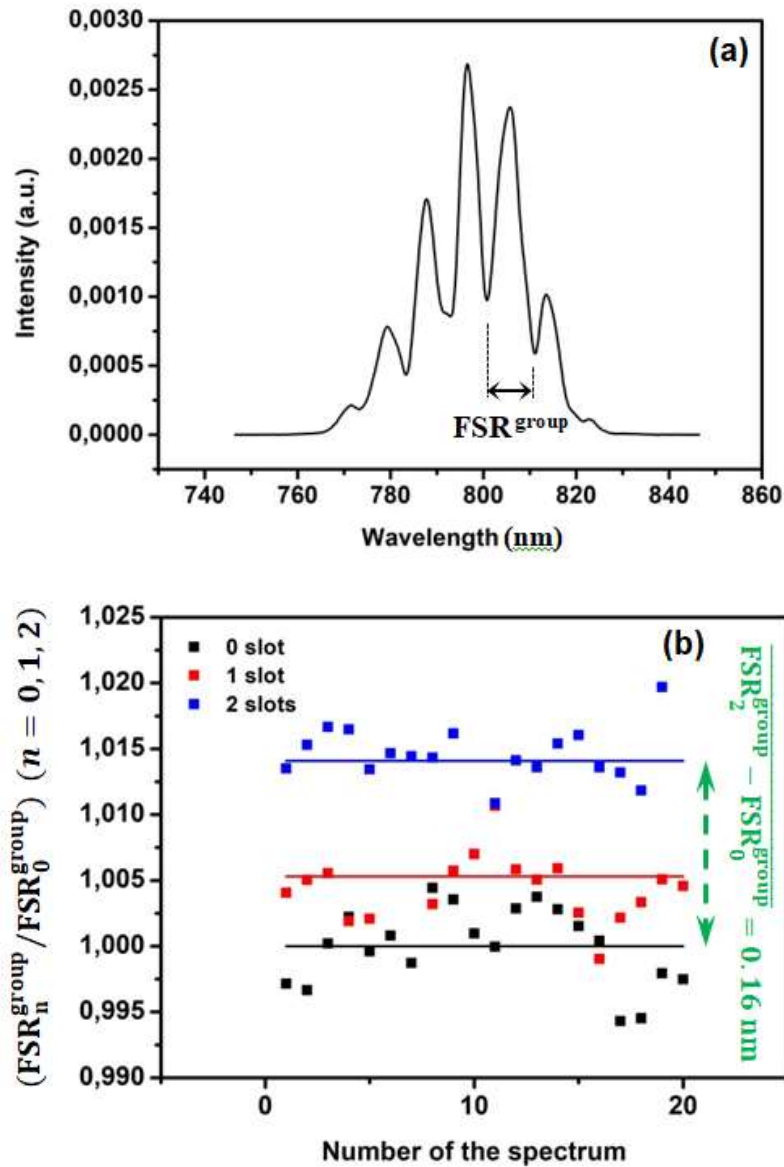
**Figure 6.** Principles and photographs of various part of the experimental setup. A broadband laser source is used to excite the slot MRs structures ( $\lambda_{0-center} = 800$  nm). The quantified light is then sent to an Optical Spectrum Analyzer (OSA). The surface of the chip is highlighted due to imaging from above. A specific software controls the whole set of data acquisitions together with the signal processing of spectra in real time.

source of light. Then, all the aforementioned dispersion aspects will be integrated into the measurements. This appliance allows us to visualize the resonances over the optical wavelength range of 780 to 820] nm. The central part of the figure is dedicated to the optical injection involving piezoelectric positioners (PI), microscope objectives plus an imaging device in top view (MBP Newport and CCD camera): the latter allows us to visualize the propagation and the coupling into the resonators without and with slots (Figure 6, bottom middle). Finally, a third part (with the dashed box) summarizes the spectral detection protocol: a specific Matlab code allows us to control the Optical Spectral Analyser (OSA) as well as the data acquisition, together with the resonance signal processing performed in real time for the  $FSR^{group}$  calculation (Figure 6, left).

**EXPERIMENTAL RESULTS AND DISCUSSION**

Relevant measurements carried out on the three types of investigated structures are depicted in Figure 7, with a given resonance spectrum, by way of example. Each set of resonances, resulting from the condition and cyclic circulation of light within the resonator, are inscribed in the Gaussian envelope of the source. The  $FSR^{group}$  stands for the pseudo-period of the signal that can be quantitatively inferred from a fast Fourier tranform (FFT). Then, we proceed with a statistic on 20 spectra to

calculate each  $FSR_{nslots}^{group}$  value ( $n = 0, 1, 2$ ), considering respectively the structures without slit ( $n=0$ ), then with one and two slits ( $n=1$  and  $2$ ). Figure 7b specifies measured values being normalized to the average  $FSR_{0slot}^{group}$ . We thus notice that such a normalized quantity ( $FSR_{2slots}^{group}/FSR_{0slot}^{group}$ ), which is equal to  $(n_{eff\_0slot}^{group}/n_{eff\_2slots}^{group})$  as mentioned previously, is markedly increased with the number of slots (without, one, then two). Hence, this optical quantity, validating the resonant principle measurement, displays a dynamic evolution from 1 to 1.015 as shown in Figure 7b, with a change close to 1.5%, corresponding to a  $33.1 \mu m^3$  recessed volume (lack of matter) considering the two inscribed nano-slots. According to the previous simulations, it may be noted that as a first slit is shaped into the structure (13% of the volume of the guide), a detection mechanism is already made possible by a surface resonant principle, the previous normalized quantity varying from 1 to 1,005 (on a statistical average of 20 acquired spectra). As detected in Figure 7 and Table 1 (experimental with notion of effective group index  $n_{eff}^{group}$  due to the broadband laser), a resonant signal of surface light is susceptible to measure a preformed lack of material. If we consider the ratio of increase or the relative fraction ( $FSR_{2slots}^{group}/FSR_{0slot}^{group}$ ) the spectral statistics measurements carried out with such organic structures evolve in the same direction with the lack of matter or



**Figure 7.** (a) Example of a spectrum transduced by a MR structure. Free Spectral Range ( $FSR_{group}$ ) represents the pseudo-period of the spectrum signal. (b) Calculation of  $FSR_n^{group}$  ( $n = 0, 1$  and 2 slots) normalized to the average of  $FSR_0^{group}$ . Such averages are determined on a 20 experimental spectra statistic.

lack of density in the core (Table 1). Moreover, a relevant adequacy of the impact of a given lack of material in the core of the waveguide on the eigenvalue evolution  $n_{eff}^{group}$  is observed. Then, considering two simulation approaches, a decrease in the effective index is brought about by a lack of material, entailing therefore an increase in  $FSR_{group}$  for the investigated regime.

Deviations from the ratio  $(FSR_{2slots}^{group} / FSR_{0slot}^{group})$  measured by experimental method and simulations  $I_{2D}$  and  $II_{3D}$  converge, respectively close to 0.39 and 0.09%. Such circumstances may inform about the portion of the void localization within the material or the lack of matter.

In all cases, this medium stratified by slits and filled with air, will indeed show off a lower index (in the sense

**Table 2.** Fabrication of global integrated circuits; parameters (speed  $v$ , acceleration  $a$ , time  $t$ , temperature "teta", energy  $E$ ) used to shape one or two slots with 400 nm width inscribed.

Step 1	Step 2	Step 3	Step 4
Spin-coating (UV210 polymer, 1 $\mu\text{m}$ ): $v = 900$ rpm, $a = 5000$ rpm/s, $t = 30$ s	Softbake: $t = 3$ min, $\theta = 140^\circ\text{C}$	Exposure (Deep UV, 248 nm): $T = 30$ s, $E = 20$ mJ/cm <sup>2</sup>	Softbake&Development (Microposit MF CD-26): $t = 1$ min, $\theta = 120^\circ\text{C}$ , $t = 30$ s

of approximations of the effective medium theory (EMT)), and therefore an increased  $\text{FSR}^{\text{group}}$  parameter. It is clear that such behaviors (measured then simulated) on this media with air slots also follow an empirical Gladstone law, namely:  $\frac{n_{\text{eff}}^{\text{group}} - 1}{\rho} = \text{constant}$ . Then, the effective medium being aerated and less dense, its optical index is decreased while the ratio remains constant.

## Conclusion

Such approach put forth a possible kind of 'photonic balance' based on a resonant principle allowing measurements of a mass differential (including mass loss). Thus, this work reports the study of the impact of a given lack of pre-formed material into a core waveguide. In order to estimate an appropriate range of dimensions characterizing the presence of vacuum (or lack of nano-slits material) that could be detectable, we implement simulations of relevant resonant structures, thanks to the COMSOL software. These simulations and theoretical approach made it possible to consider an effective detection of specific recessed volume starting at relevant void volumes with respective percentages close to 10% of the MR volume. To this end we have taken advantage of nanotechnology processes based on deep UV lithography (248 nm) applied to organic materials. The UV 210 polymer was thus processed so as to shape specific slots within a set of waveguides. Then, the latter have been re-looped as micro-resonators circuits with a view to first creating the resonant signal prior measurements of the relevant variations of the pseudo-period  $\text{FSR}^{\text{group}}$ . Observed changes are associated to the resonances directly linked (inversely proportional) to the eigenvalue  $n_{\text{eff}}^{\text{group}}$  characterizing the electromagnetism propagation. Experiments allowed us to highlight such changes in effective indices as clearly correlated to the amount of void. With the realized organic devices, specific resonant experimental measurements have been compared with relevant electromagnetic simulations; then, results proved to corroborate the expected evolution on the eigenvalue of the system. As the lack of material reaches 10% (imprinted within space and extended to the re-circulating light field), a noticeable variation may be observed.

Such measurements allowed us to confirm the

measured evolution in agreement with the associated simulations (COMSOL software, respectively I\_2D and II\_3D) to the nearest 0.09-039% regarding the relative ratio ( $\text{FSR}_{2\text{slots}}^{\text{group}}/\text{FSR}_{0\text{slot}}^{\text{group}}$ ). In conclusion, considering a given lack of material, either above or within the guide, the resonant signal is clearly altered, as a consequent modification of the eigenvalue  $n_{\text{eff}}^{\text{group}}$  and its relevant  $\text{FSR}^{\text{group}}$  resonant quantity; this study provides a way to evaluate the global dynamic ranging effect due to a given mass hollowed out (nano-gap of air) from the considered looped structures by way of assessing the entailed spectral signature.

## CONFLICT OF INTERESTS

The authors have not declared any conflict of interests.

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