Full Length Research Paper

# Prediction of stress concentration effect under thermal and dynamic loads in a high pressure turbine rotor

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Geometric discontinuities cause a large variation of stress and produce a significant increase in stress. The high stress due to the variation of geometry is called as 'stress concentration'. This will increase when the loads are further applied. There are many investigators who studied the stress distribution around the notches, grooves, and other irregularities of various machine components. This paper analyses the effect of stress concentration under thermal and dynamic loads in a steam turbine rotor grooves under the operating conditions. Stresses due to thermal and dynamic loads in high pressure steam turbine rotor of 210 MW power station were found in two stages. A source code is developed for calculating the nominal stress at each groove section of HPT rotor. Maximum stress is obtained using FEA at the corresponding section. Stress concentration factors due to thermal and dynamic loads at each section were calculated. It is observed that the stress concentration due to the combined effect of thermal and dynamic loads is exceeding the safe limits at temperatures beyond 540 °C.

Key words: Stress concentration factors, HPT rotor, thermal loads, dynamic loads.

## INTRODUCTION

Peterson (1958) did a significant research on stress concentration of various machine components. Neuber (1961) did an exhaustive work on stress concentration factors for extreme thin components. Alexander and Leyzerovich (2007) found that cycling thermal stresses or low-cycle fatigue on steam turbine rotor exceeds prescribed limits that can lead to cracking of the rotors. Gee et al. (2006) worked on the thermal stresses of steam turbines and observed that these are due to the steam flow temperature. Kang and Jong (1996) found that stress intensity factor (SIF) for an embedded elliptical crack in a turbine rotor and thermal shock stress intensity factor for a semi-elliptical surface crack in a finite plate are determined by numerical methods. Shlyannikov et al. (2008) assessed the integrity of cracked steam turbine rotor which operates under creep conditions. Kostyuk (2006) verified results from calculating the long-term strength of single-piece forged rotors using the natural

mechanistic procedure are compared with the experimental long-term strength characteristics of the models of high-temperature disk rims and with the field data on failures of such rims.

The contributions of the above in this area are very useful for many investigations. In the literature, it is not available for the cases like determining the stress concentration factors for critical and heavy components such as turbine rotors. Most of the researchers concentrated or limited their works to only one type of analysis such as either static or thermal or dynamic load.

In recent years, there has been an increased interest in the design and analysis of steam and gas turbines. In the power plant applications, a steam turbine rotor is indispensable equipment for power generation. The life of rotors in steam turbines has a severe impact on the power generation system. In the present work, a typical HP turbine rotor considered for the determination of stress concentration factors is described. A theoretical investigation of the turbine rotor using finite element method has been presented. Thermal and dynamic stresses are obtained using finite element analysis.

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Figure 1. Line drawing of HPT rotor.



Figure 2. Plane 182 element.



Figure 3. FE model of HP turbine rotor.

Stress concentration factors for thermal and dynamic loads are calculated for HP rotor.

#### DESCRIPTION

A line diagram of HPT rotor is presented in Figure 1. The geometric and elastic properties and also operating conditions are as follows:

Rated output = 210 MW Rated speed = 3000 rpm Inlet steam pressure =150 kg/cm<sup>2</sup> (absolute) Inlet steam temperature =  $535 \,^{\circ}$ C Reheat steam temperature =  $535 \,^{\circ}$ C Weight of the unit = 475 tons Overall length = 16.975 m Overall width = 10.5 m Rated frequency = 50 c/s Maximum permissible speed = 3090 rpm Minimum permissible speed = 2850 rpm Maximum frequency = 51.5 c/s Minimum frequency = 47.5 c/s

#### MODELING OF THE PROBLEM

The chosen problem is considered as 2-D axi-symmetric problem to reduce the considerable time of computations and tedious computer efforts. The model consists more than 10,000 elements. Figure 2 shows the element 182 considered for meshing. FE modeling of the HP turbine rotor is shown in the Figure 3. Appropriate boundary conditions are incorporated in the analysis. The element can be used as either a plane element (plane stress, plane strain or generalized plane strain) or an axisymmetric element. Axi-symmetric elements are available in most finite element packages and in a range of element shapes and types. No special boundary conditions have to be applied to these elements to achieve the symmetry condition. It is defined by four nodes having two degrees of freedom at each node: Translations in the nodal x and y directions. The element has plasticity, hyper elasticity, stress stiffening, large deflection, and large strain capabilities. It also has mixed formulation capability for simulating deformations of nearly incompressible elastoplastic materials, and fully incompressible hyper elastic materials.

Stress concentration factors for thermal and dynamic loads are computed in terms of stresses developed due to static loading on the rotors, load that is developed due to temperature rise and the load acting on the turbine blades due to steam pressure.

0		Thermal stress (N/m <sup>2</sup> ) ×10 <sup>6</sup>								
Groove no.	530 <i>°</i> C	535 ℃	540 <i>°</i> C	545 ℃	550 ℃					
1	2.229249	2.408066	2.598804	2.801463	3.027964					
2	2.422833	2.616144	2.822343	3.054316	3.299177					
3	2.632442	2.839178	3.059697	3.307780	3.569646					
4	2.804383	3.023476	3.271780	3.534691	3.812208					
5	2.994934	3.225314	3.486410	3.762866	4.070039					
6	3.143808	3.400445	3.657083	3.961840	4.282636					
7	3.296652	3.563048	3.846093	4.162439	4.495434					
8	3.437682	3.712696	4.004899	4.331479	4.675247					
9	3.566470	3.866618	4.166767	4.502227	4.855343					
10	3.682588	3.971418	4.296352	4.639338	5.000376					
11	3.785610	4.098014	4.428796	4.777954	5.163865					
12	3.893735	4.210450	4.545795	4.899771	5.291008					
13	3.950646	4.270460	4.609087	4.985339	5.380403					
14	4.030731	4.352432	4.693057	5.071529	5.487849					
15	4.077125	4.418466	4.759806	5.139074	5.556268					
16	4.108211	4.430052	4.789757	5.168394	5.584894					
17	4.123563	4.462486	4.820238	5.196819	5.611058					
18	4.141408	4.477198	4.831643	5.223397	5.633807					
19	4.105353	4.436727	4.786510	5.173113	5.596535					
20	4.089028	4.414703	4.758471	5.138425	5.554565					
21	4.036775	4.373173	4.709571	5.099085	5.506303					
22	3.966582	4.277010	4.621930	4.984097	5.398001					
23	3.878015	4.195611	4.529923	4.897665	5.282124					
24	3.786762	4.092926	4.415204	4.769709	5.156442					
25	3.659498	3.952875	4.277134	4.616834	4.987416					

Table 1. Groove number Vs thermal stresses.

#### The software

The problem is analyzed by the software ANSYS 10.0. The flexibility, capability and options made the ANSYS program as user oriented and can be applied to variety of practical problems. The package contains many routines and all are interrelated to achieve a solution to the practical problems by finite element method.

#### **RESULTS AND DISCUSSION**

The rotor is cut with 25 grooves stretching over a span of 1.712 m to accommodate the blades. The analysis has been carried-out in two phases. The 1<sup>st</sup> phase involves thermal analysis and the 2<sup>nd</sup> phase covers dynamic analysis.

#### Thermal analysis

Variation of thermal stresses with respect to grooves is shown in Table 1. The results are plotted in Figure 4. Theoretical stress concentration factor based on thermal stress is given in Table 2 and plotted in Figure 5. The way the theoretical stress concentration factor is varying with respect of thermal stresses is shown in the Table 3 and plotted in Figure 6. The thermal stresses are obtained at the elevated temperatures of 530, 535, 540, 545 and  $550 \,^{\circ}$ C.

It is observed that thermal stresses are increasing from 2.229249 × 10<sup>6</sup> N/m<sup>2</sup> to 4.141408 × 10<sup>6</sup> from the 1<sup>st</sup> to 18<sup>th</sup> groove and gradually decreasing to 3.659498 × 10<sup>6</sup> N/m<sup>2</sup> at the temperature of 530 °C. At 535 °C, thermal stresses are 2.408066 × 10<sup>6</sup> N/m<sup>2</sup> at the 1<sup>st</sup> groove and gradually decreasing to a value of 3.952875 × 10<sup>6</sup> N/m<sup>2</sup> at 25<sup>th</sup> groove. At 540 °C, thermal stresses are 2.598804 × 10<sup>6</sup> N/m<sup>2</sup> at the 1<sup>st</sup> groove and gradually increasing to a value of 4.277134 × 10<sup>6</sup> N/m<sup>2</sup> to the last groove. It is observed that thermal stresses are increasing 2.801463 × 10<sup>6</sup> to 5.223397 × 10<sup>6</sup> N/m<sup>2</sup> from the 1<sup>st</sup> to 18<sup>th</sup> groove and gradually decreasing to a value of 4.616834 × 10<sup>6</sup> N/m<sup>2</sup> to the last groove at the temperature of 545 °C. It is observed that the thermal stresses are increased 3.027964 × 10<sup>6</sup> to 5.633807 × 10<sup>6</sup> N/m<sup>2</sup> to the 1<sup>st</sup> to 18<sup>th</sup> groove to the value of 4.987416×10<sup>6</sup> N/m<sup>2</sup> at the



Figure 4. Variation of thermal stresses with respect to groove.

Table 2. Thermal stress vs.	theoretical stress	concentration	factor.
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Creation ma		Thermal stress (N/m <sup>2</sup> ) ×10 <sup>6</sup>						Theoretical stress concentration factor (Kt)			
Groove no.	530 °C	535 °C	540 °C	545 ℃	550 ℃	530 <i>°</i> C	535 <i>°</i> C	540 <i>°</i> C	545 <i>°</i> C	550 °C	
1	2.229249	2.408066	2.598804	2.801463	3.027964	1.7	1.84	1.98	2.14	2.31	
2	2.422833	2.616144	2.822343	3.054316	3.299177	1.71	1.85	1.99	2.15	2.33	
3	2.632442	2.839178	3.059697	3.307780	3.569646	1.74	1.87	2.02	2.18	2.35	
4	2.804383	3.023476	3.271780	3.534691	3.812208	1.75	1.88	2.04	2.2	2.37	
5	2.994934	3.225314	3.486410	3.762866	4.070039	1.77	1.91	2.06	2.23	2.41	
6	3.143808	3.400445	3.657083	3.961840	4.282636	1.78	1.93	2.07	2.25	2.43	
7	3.296652	3.563048	3.846093	4.162439	4.495434	1.8	1.95	2.1	2.27	2.45	
8	3.437682	3.712696	4.004899	4.331479	4.675247	1.82	1.96	2.12	2.29	2.47	
9	3.566470	3.866618	4.166767	4.502227	4.855343	1.84	1.99	2.15	2.32	2.5	
10	3.682588	3.971418	4.296352	4.639338	5.000376	1.85	2	2.16	2.34	2.52	
11	3.785610	4.098014	4.428796	4.777954	5.163865	1.87	2.03	2.19	2.36	2.55	
12	3.893735	4.210450	4.545795	4.899771	5.291008	1.9	2.05	2.22	2.39	2.58	
13	3.950646	4.270460	4.609087	4.985339	5.380403	1.91	2.06	2.23	2.41	2.6	
14	4.030731	4.352432	4.693057	5.071529	5.487849	1.94	2.09	2.25	2.44	2.64	
15	4.077125	4.418466	4.759806	5.139074	5.556268	1.95	2.12	2.28	2.46	2.66	
16	4.108211	4.430052	4.789757	5.168394	5.584894	1.97	2.13	2.3	2.48	2.68	
17	4.123563	4.462486	4.820238	5.196819	5.611058	1.99	2.15	2.33	2.51	2.71	
18	4.141408	4.477198	4.831643	5.223397	5.633807	2.02	2.18	2.35	2.55	2.75	
19	4.105353	4.436727	4.786510	5.173113	5.596535	2.03	2.19	2.36	2.55	2.76	
20	4.089028	4.414703	4.758471	5.138425	5.554565	2.05	2.22	2.39	2.58	2.79	
21	4.036775	4.373173	4.709571	5.099085	5.506303	2.07	2.25	2.42	2.62	2.83	
22	3.966582	4.277010	4.621930	4.984097	5.398001	2.09	2.25	2.44	2.63	2.85	
23	3.878015	4.195611	4.529923	4.897665	5.282124	2.11	2.28	2.46	2.66	2.87	
24	3.786762	4.092926	4.415204	4.769709	5.156442	2.14	2.31	2.49	2.69	2.91	
25	3.659498	3.952875	4.277134	4.616834	4.987416	2.15	2.33	2.52	2.72	2.94	



Figure 5. Theoretical stress concentration factor with respect to thermal stress.

Groove no.		Theoretical st	ress concentrat	ion factor (K <sub>t</sub> )	
	530 <i>°</i> C	535 <b>℃</b>	540 <i>°</i> C	545 <i>°</i> C	550 <i>°</i> C
1	1.7	1.84	1.98	2.14	2.31
2	1.71	1.85	1.99	2.15	2.33
3	1.74	1.87	2.02	2.18	2.35
4	1.75	1.88	2.04	2.2	2.37
5	1.77	1.91	2.06	2.23	2.41
6	1.78	1.93	2.07	2.25	2.43
7	1.8	1.95	2.1	2.27	2.45
8	1.82	1.96	2.12	2.29	2.47
9	1.84	1.99	2.15	2.32	2.5
10	1.85	2	2.16	2.34	2.52
11	1.87	2.03	2.19	2.36	2.55
12	1.9	2.05	2.22	2.39	2.58
13	1.91	2.06	2.23	2.41	2.6
14	1.94	2.09	2.25	2.44	2.64
15	1.95	2.12	2.28	2.46	2.66
16	1.97	2.13	2.3	2.48	2.68
17	1.99	2.15	2.33	2.51	2.71
18	2.02	2.18	2.35	2.55	2.75
19	2.03	2.19	2.36	2.55	2.76
20	2.05	2.22	2.39	2.58	2.79
21	2.07	2.25	2.42	2.62	2.83
22	2.09	2.25	2.44	2.63	2.85
23	2.11	2.28	2.46	2.66	2.87
24	2.14	2.31	2.49	2.69	2.91
25	2.15	2.33	2.52	2.72	2.94

**Table 3.** Grove number vs. theoretical stress concentration factor.



Figure 6. Variation of theoretical stress concentration factor with respect to groove.

Table 4. Groove number Vs dynamic stresses.

Dynamic stresses (N/m <sup>2</sup> ) ×10 <sup>7</sup>							
Groove no.	Operating	530 ℃	535 ℃	540 ℃	545 ℃	550 °C	
1	1.2937470	2.1037452	2.2724947	2.4524943	2.6437439	2.8574934	
2	1.4178348	2.2978702	2.4812108	2.6767743	2.8967831	3.1290147	
3	1.5348290	2.5055756	2.7023485	2.9122397	3.1483672	3.3976130	
4	1.6444978	2.6757931	2.8848394	3.1217586	3.3726142	3.6374062	
5	1.7612870	2.8620914	3.0822522	3.3317679	3.5959609	3.8895088	
6	1.8409324	3.0068563	3.2523139	3.4977715	3.7892525	4.0960745	
7	1.9431621	3.1536566	3.4084975	3.6792660	3.9818896	4.3004407	
8	2.0217210	3.2873512	3.5503393	38297641	4.1420625	4.4707976	
9	2.0917185	3.4074770	3.6942449	3.9810127	4.3015180	4.6388920	
10	2.1529227	3.5135699	37891440	4.0991648	4.4264091	4.7708767	
11	2.2226027	3.6051667	3.9026804	4.2176949	4.5502103	4.9177273	
12	2.2657251	3.6995044	4.0004209	4.3190385	4.6553571	5.0270776	
13	2.2992820	3.7430173	4.0460234	4.3668535	4.7233313	5.0976330	
14	2.3409107	3.8062136	4.1099959	4.4316477	4.7890387	5.1821687	
15	2.3546089	3.8351585	41562415	4.4773246	4.8340835	5.2265183	
16	2.3579686	3.8472120	4.1486064	4.4854591	4.8400408	5.2300807	
17	2.3683014	3.8419112	4.1576847	4.4910012	4.8418607	5.2278061	
18	2.3500257	3.8360715	4.1471042	44754167	4.8382883	5.2184395	
19	2.3206392	37773908	4.0822923	4.4041328	4.7598512	5.1494476	
20	2.2964311	3.7337657	4.0311452	4.3450458	4.6919887	5.0719737	
21	2.2436321	3.6539153	3.9584082	4.2629011	4.6154719	4.9840686	
22	2.1789498	3.5543153	3.8324791	4.1415500	4.4660744	4.8369595	
23	2.1169559	3.4345020	3.7157756	4.0118536	4.3375391	4.6780286	
24	2.0270842	3.3080888	3.5755513	3.8570908	4.1667842	4.5046316	
25	1.9378292	3.1456543	3.3978375	3.6765664	3.9685680	4.2871153	

temperature of 550 ℃.

### **Dynamic analysis**

Variation of dynamic stresses with respect to grooves is

shown in Table 4. These readings are plotted in Figure 7. Effect of dynamic stresses on fatigue stress concentration factor is given in Table 5 and plotted in Figure 8. The way the fatigue stress concentration factor is varying



Figure 7. Variation of dynamic stress with respect to groove.



Figure 8. Dynamic stress concentration factor with respect to dynamic stress.

	Table 5. D	vnamic stress	vs. fatigue stress	concentration	factor.
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Groove	Dynamic stresses (N/m <sup>2</sup> ) × 10 <sup>7</sup>						Fa	tigue stre	ss concer	ntration fa	ctor (K <sub>f</sub> )	
No.	Operating	530 <i>°</i> C	535 ℃	540 <i>°</i> C	545 <i>°</i> C	550 <i>°</i> C	Operating	530 <i>°</i> C	535 <i>°</i> C	540 <i>°</i> C	545 ℃	550 <i>°</i> C
1	1.2937470	2.1037452	2.2724947	2.4524943	2.6437439	2.8574934	1.14	1.78	1.92	2.06	2.22	2.39
2	1.4178348	2.2978702	2.4812108	2.6767743	2.8967831	3.1290147	1.14	1.79	1.93	2.07	2.23	2.4
3	1.5348290	2.5055756	2.7023485	2.9122397	3.1483672	3.3976130	1.15	1.82	1.95	2.1	2.26	2.43
4	1.6444978	2.6757931	2.8848394	3.1217586	3.3726142	3.6374062	1.16	1.83	1.96	2.12	2.28	2.45
5	1.7612870	2.8620914	3.0822522	3.3317679	3.5959609	3.8895088	1.18	1.86	1.99	2.14	2.31	2.49
6	1.8409324	3.0068563	3.2523139	3.4977715	3.7892525	4.0960745	1.18	1.86	2.01	2.15	2.32	2.5
7	1.9431621	3.1536566	3.4084975	3.6792660	3.9818896	4.3004407	1.2	1.88	2.03	2.18	2.35	2.53
8	2.0217210	3.2873512	3.5503393	3.8297641	4.1420625	4.4707976	1.21	1.9	2.04	2.2	2.37	2.55
9	2.0917185	3.4074770	3.6942449	3.9810127	4.3015180	4.6388920	1.22	1.92	2.07	2.22	2.4	2.58
10	2.1529227	3.5135699	3.7891440	4.0991648	4.4264091	4.7708767	1.23	1.94	2.08	2.24	2.41	2.59
11	2.2226027	3.6051667	3.9026804	4.2176949	4.5502103	4.9177273	1.24	1.95	2.11	2.27	2.44	2.63
12	2.2657251	3.6995044	4.0004209	4.3190385	4.6553571	5.0270776	1.25	1.98	2.13	2.3	2.47	2.66
13	2.2992820	3.7430173	4.0460234	4.3668535	4.7233313	5.0976330	1.26	1.99	2.14	2.31	2.49	2.67
14	2.3409107	3.8062136	4.1099959	4.4316477	4.7890387	5.1821687	1.28	2.02	2.17	2.33	2.51	2.71
15	2.3546089	3.8351585	4.1562415	4.4773246	4.8340835	5.2265183	1.29	2.04	2.2	2.36	2.54	2.74
16	2.3579686	3.8472120	4.1486064	4.4854591	4.8400408	5.2300807	1.3	2.05	2.21	2.38	2.56	2.76
17	2.3683014	3.8419112	4.1576847	4.4910012	4.8418607	5.2278061	1.32	2.07	2.23	2.4	2.58	2.78
18	2.3500257	3.8360715	4.1471042	4.4754167	4.8382883	5.2184395	1.32	2.1	2.26	2.43	2.62	2.82
19	2.3206392	3.7773908	4.0822923	4.4041328	4.7598512	5.1494476	1.33	2.11	2.27	2.44	2.63	2.84
20	2.2964311	3.7337657	4.0311452	4.3450458	4.6919887	5.0719737	1.35	2.13	2.3	2.47	2.66	2.86
21	2.2436321	3.6539153	3.9584082	4.2629011	4.6154719	4.9840686	1.36	2.15	2.32	2.49	2.69	2.9
22	2.1789498	3.5543153	3.8324791	4.1415500	4.4660744	4.8369595	1.37	2.17	2.33	2.51	2.7	2.92
23	2.1169559	3.4345020	3.7157756	4.0118536	4.3375391	4.6780286	1.39	2.19	2.36	2.54	2.74	2.94
24	2.0270842	3.3080888	3.5755513	3.8570908	4.1667842	4.5046316	1.4	2.22	2.39	2.57	2.76	2.98
25	1.9378292	3.1456543	3.3978375	3.6765664	3.9685680	4.2871153	1.41	2.23	2.4	2.59	2.79	3.01

with respect to dynamic stresses is shown in the Table 6. These readings are plotted in Figure 9. The dynamic stresses are obtained by considering self weight of rotor, blade weight and steam load as uniformly distributed load over a span of 1.712 m at the operating and also elevated temperatures of 530, 535, 540, 545 and 550 °C.

It is observed that dynamic stresses are increasing

increasing from 1.2937470 ×  $10^7$  to 23683014 N/m<sup>2</sup> from the 1<sup>st</sup> to 17<sup>th</sup> groove and gradually decreasing to a value of 1.9378292 ×  $10^7$  N/m<sup>2</sup> to a last groove of 25<sup>th</sup> at the operating temperature. It is observed that the dynamic stresses increased from 2.1037452 ×  $10^7$  to 3.8472120 ×  $10^7$  N/m<sup>2</sup> from the 1<sup>st</sup> to 16<sup>th</sup> groove and gradually decreasing to 25th groove to a value of 3.1456543

 $\times$  10<sup>7</sup> N/m<sup>2</sup> at the temperature of 530 °C. At the temperature 535 °C, dynamic stresses are 2.2724947  $\times$  10<sup>7</sup> N/m<sup>2</sup> at the 1<sup>st</sup> groove and gradually increasing to 4.1576847  $\times$  10<sup>7</sup> N/m<sup>2</sup> up to 17<sup>th</sup> groove and gradually decreasing to 3.3978375  $\times$  10<sup>7</sup> N/m<sup>2</sup> to the last groove of 25<sup>th</sup> groove. It is observed that dynamic stresses increased from 2.4524943  $\times$  10<sup>7</sup> to 4.4910012  $\times$ 

<b>O</b> re over me	Fatigue stress concentration factor (K <sub>f</sub> )									
Groove no.	Operating	530 <i>°</i> C	530 <i>°</i> C	535 °C	540 <i>°</i> C	545 <i>°</i> C				
1	1.14	1.78	1.92	2.06	2.22	2.39				
2	1.14	1.79	1.93	2.07	2.23	2.4				
3	1.15	1.82	1.95	2.1	2.26	2.43				
4	1.16	1.83	1.96	2.12	2.28	2.45				
5	1.18	1.86	1.99	2.14	2.31	2.49				
6	1.18	1.86	2.01	2.15	2.32	2.5				
7	1.2	1.88	2.03	2.18	2.35	2.53				
8	1.21	1.9	2.04	2.2	2.37	2.55				
9	1.22	1.92	2.07	2.22	2.4	2.58				
10	1.23	1.94	2.08	2.24	2.41	2.59				
11	1.24	1.95	2.11	2.27	2.44	2.63				
12	1.25	1.98	2.13	2.3	2.47	2.66				
13	1.26	1.99	2.14	2.31	2.49	2.67				
14	1.28	2.02	2.17	2.33	2.51	2.71				
15	1.29	2.04	2.2	2.36	2.54	2.74				
16	1.3	2.05	2.21	2.38	2.56	2.76				
17	1.32	2.07	2.23	2.4	2.58	2.78				
18	1.32	2.1	2.26	2.43	2.62	2.82				
19	1.33	2.11	2.27	2.44	2.63	2.84				
20	1.35	2.13	2.3	2.47	2.66	2.86				
21	1.36	2.15	2.32	2.49	2.69	2.9				
22	1.37	2.17	2.33	2.51	2.7	2.92				
23	1.39	2.19	2.36	2.54	2.74	2.94				
24	1.4	2.22	2.39	2.57	2.76	2.98				
25	1.41	2.23	2.4	2.59	2.79	3.01				

Table 6. Groove number vs. fatigue stress concentration factor.



Figure 9. Variation of dynamic stress concentration factor with respect to groove.

10<sup>7</sup> N/m<sup>2</sup> from the 1st to the 17<sup>th</sup> groove and gradually decreasing to 3.6765664 × 10<sup>7</sup> N/m<sup>2</sup> at the temperature of 540 °C. At the temperature of 545 °C, dynamic stresses were 2.6437439 × 10<sup>7</sup> N/m<sup>2</sup> at the 1<sup>st</sup> groove and gradually increasing to 4.8418607 × 10<sup>7</sup> N/m<sup>2</sup> up to 17<sup>th</sup> groove and gradually decreasing to 3.9685680 × 10<sup>7</sup> N/m<sup>2</sup> to 25<sup>th</sup> groove. It is observed that the dynamic stresses increased from 2.8574934 ×10<sup>7</sup> to 5.2300807 × 10<sup>7</sup> N/m<sup>2</sup> from the 1<sup>st</sup> to the 16<sup>th</sup> groove and gradually decreasing to the 25th groove to a value of 4.2871153 × 10<sup>7</sup> N/m<sup>2</sup> at the temperature of 550 °C.

#### Conclusion

In this study, an attempt was made to compute stress concentration factors due to thermal and fatigue loadings. The methodology adopted gives a systematic theoretical investigation to predict high concentration of stress and its impact on the life of the rotor. At the end of the analysis, it is concluded that at 545 °C there will be a high concentration of stress and hence it is suggested to operate the turbine corresponding to inlet steam temperature which is less than 545 °C.

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